Learning Chaotic and Stochastic Dynamics from Noisy and Partial Observation using Variational Deep Learning
Duong Nguyen, Said Ouala, Lucas Drumetz, Ronan Fablet

To cite this version:
Duong Nguyen, Said Ouala, Lucas Drumetz, Ronan Fablet. Learning Chaotic and Stochastic Dynamics from Noisy and Partial Observation using Variational Deep Learning. CT'2020: 10th International Conference on Climate Informatics, Sep 2020, Oxford, United Kingdom. hal-02941313

HAL Id: hal-02941313
https://imt-atlantique.hal.science/hal-02941313
Submitted on 16 Sep 2020

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Learning Chaotic and Stochastic Dynamics from Noisy and Partial Observation Using Variational Deep Learning

Duong Nguyen¹, Said Ouala¹, Lucas Drumetz¹ and Ronan Fablet¹

I. CONTEXT AND PROPOSED APPROACH

Although many works have recently successfully provided proofs of concept for data driven approaches of learning dynamical systems under ideal conditions, i.e. noise-free and high sampling frequency, dealing with real life data where the measurements are usually noisy and can be partially and irregularly sampled remains challenging.

We propose a new method, called DAODEN (Data-Assimilation-based Ordinary Differential Equation Network), which can explicitly capture the stochastic components of both the process of interest and the observation system. It involves two main modules: an inference module which aims to reconstruct the hidden states of the systems from damaged observations, and a generative model which addresses the dynamics of the system and the observation model. The proposed learning strategy relies on a variational learning setting. By construction, it guarantees performance similar to state-of-the-art schemes under ideal experimental settings.

Specifically, given a series of observations $x_{1:T}$, which can be noisy, partially and irregularly sampled of a dynamical system, DAODEN supposes that the generation process of $x_{1:T}$ relies on a series of true states $z_{1:T}$. The inference module in DAODEN is an LSTM-based network that reconstructs $z_t$ from $x_{1:T}$: $q_\phi(z_t|x_{1:T})$. The generative module involves the parametrization of the dynamics of the hidden states $p_\theta(z_{t+1}|z_t)$, modeled by a neural network; and an observation distribution $p(x_k|z_k)$, usually known. DAODEN maximizes the Evidence Lower BOUND (ELBO) of the log likelihood $\ln p(x_{1:T})$ over $\{\theta, \phi\}$. This optimization results in the surrogate model of the dynamics of the considered system.

II. EXPERIMENT AND RESULT

As illustration of the proposed framework, we first consider an application to the identification of an ODE representation given noisy and irregularly sampled observations, here for Lorenz-63 system. Using a Bilinear Neural Network (BiNN) [1] for the dynamical module, we show that DAODEN significantly outperforms the direct learning of the BiNN model from the observation data both in the short-term prediction error and the long-term topology.

Compared with previous works, DAODEN can also capture the stochasticity of dynamical systems, such as in the Lorenz 63 stochastic system [2], as presented in Fig. 1.

TABLE I: Short term prediction error ($e_4$) and the first Lyapunov exponent ($\lambda_1$) of models trained on noisy and partially observed Lorenz63 data with a missing rate of 80%. The results are averaged over 50 test sequences.

<table>
<thead>
<tr>
<th>Model</th>
<th>$std_{\text{noise}}/std_{\text{signal}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>BiNN</td>
<td></td>
</tr>
<tr>
<td>$e_4$</td>
<td>0.348±0.327</td>
</tr>
<tr>
<td>$\lambda_1$</td>
<td>1.116±0.026</td>
</tr>
<tr>
<td>DAODEN</td>
<td></td>
</tr>
<tr>
<td>$e_4$</td>
<td>0.089±0.062</td>
</tr>
<tr>
<td>$\lambda_1$</td>
<td>0.892±0.011</td>
</tr>
</tbody>
</table>

Fig. 1: Attractors generated by the true Lorenz63 stochastic system (top), and by DAODEN (bottom). The true Lorenz63 stochastic system and DAODEN system are stochastic, hence each runtime we obtain a different sequence, even with the same initial condition. The model was trained on noisy observations, with a noise level of 33.3%.

REFERENCES


¹IMT Atlantique, Lab-STICC, 29238 Brest, France