

# EMMI Rapid Reaction Task Force

GSI, 18-22 July 2016

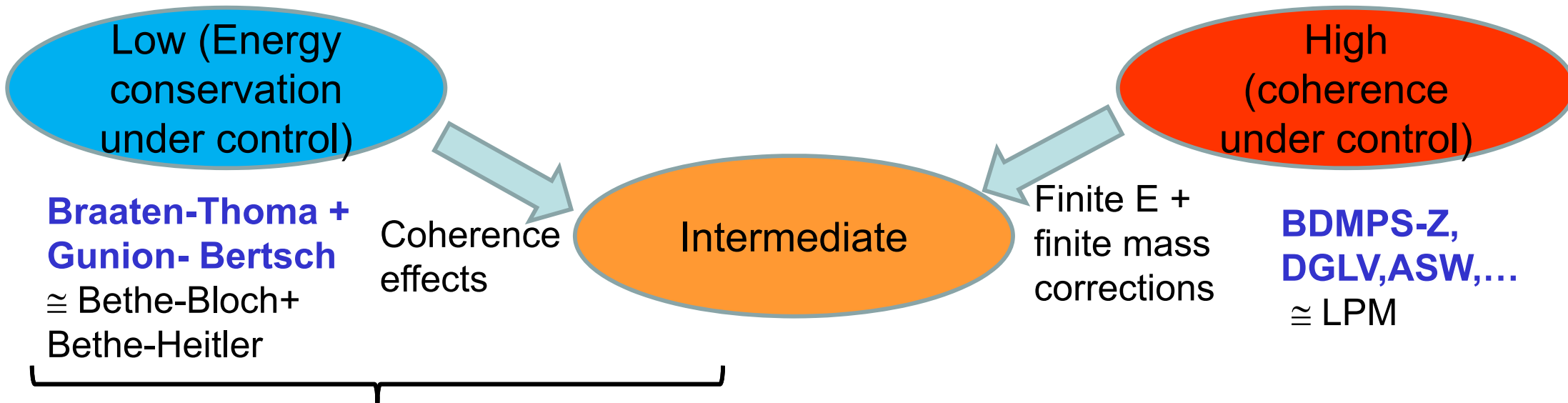
Microscopic Models of  
Energy Loss and transport coefficients:  
The Nantes Approach

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# Motivation and context

- Most of the *interesting* HF observables so far: located at *intermediate*  $p_T$   
( $\approx 3$  GeV-50 GeV)
- Intermediate  $p_T$ : hope that pQCD (or pQCD inspired models) apply (as compared to low  $p_T$ )
- Intermediate  $p_T$ : mass effect still present and thus hope to learn something more as compared to large  $p_T$

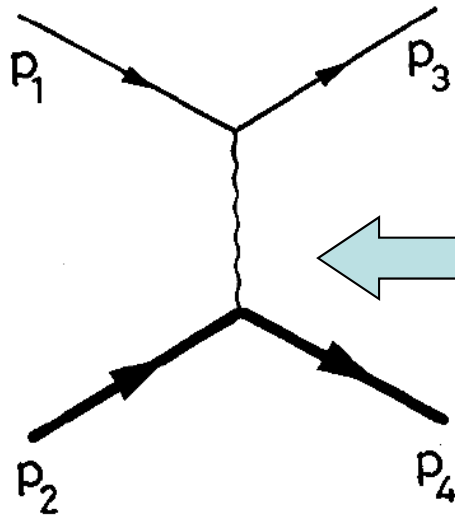


Approach pursued in our **models**... Unfortunately too many of them

=> Need for falsification (more observables; IQCD): **Azimuthal correlations<sub>2</sub>**?

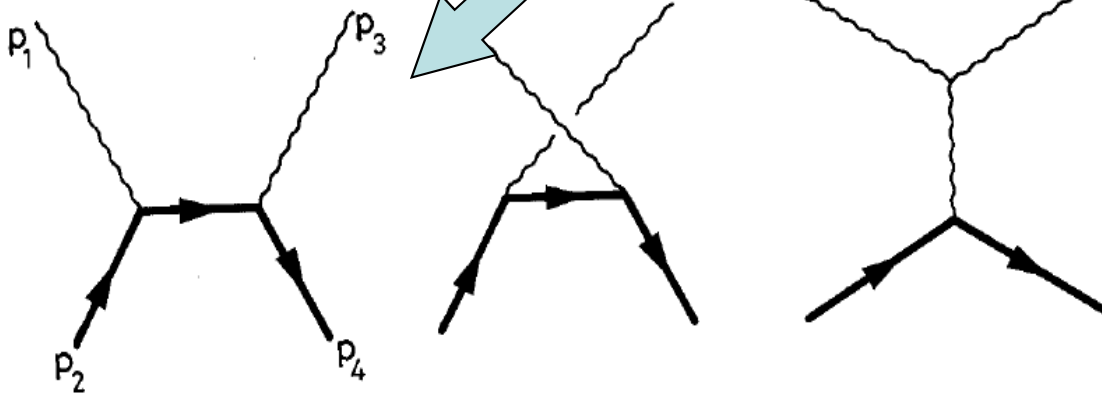
# Cross sections

Starting from Cambridge (79) as a basis:



$$\Sigma |m|^2 = \frac{64\pi^2 \alpha^2(Q^2)}{9} \frac{(M^2-u)^2 + (s-M^2)^2 + 2M^2t}{t^2}$$

$$\Sigma |m|^2 = \pi^2 \alpha^2(Q^2) \left[ \frac{32(s-M^2)(M^2-u)}{t^2} + \frac{64(s-M^2)(M^2-u) + 2M^2(s+M^2)}{9(s-M^2)^2} \right. \\ \left. + \frac{64(s-M^2)(M^2-u) + 2M^2(M^2+u)}{9(M^2-u)^2} + \frac{16M^2(4M^2-t)}{9(s-M^2)(M^2-u)} \right. \\ \left. + 16 \frac{(s-M^2)(M^2-u) + M^2(s-u)}{t(s-M^2)} - 16 \frac{(s-M^2)(M^2-u) - M^2(s-u)}{t(M^2-u)} \right]$$



However, t-channel is IR divergent  $\Rightarrow$  model **S**

## Naïve regulating of IR divergence:

$$\frac{1}{t} \longrightarrow \frac{1}{t - \mu^2}$$

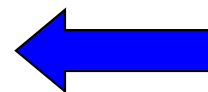
With  $\mu(T)$  or  $\mu(t)$

OBE model, NOT pQCD at finite T !!!

## Models A/B: 2 customary choices

$$\mu^2(T) = m_D^2 = 4\pi\alpha_s(1+3/6)T^2$$

$$\alpha_s(Q^2) \rightarrow \begin{cases} 0.3 \text{ (mod A)} \\ \alpha_s(2\pi T) \text{ (mod B)} (\approx 0.3) \end{cases}$$



(Svetitsky: 0.5; equil time of 1fm/c) !!!

$$\frac{dE_{coll}(c)}{dx}$$

T (MeV) \ p (GeV/c)	10	20
200	0.18	0.27
400	0.35	0.54

... of the order of a few % !

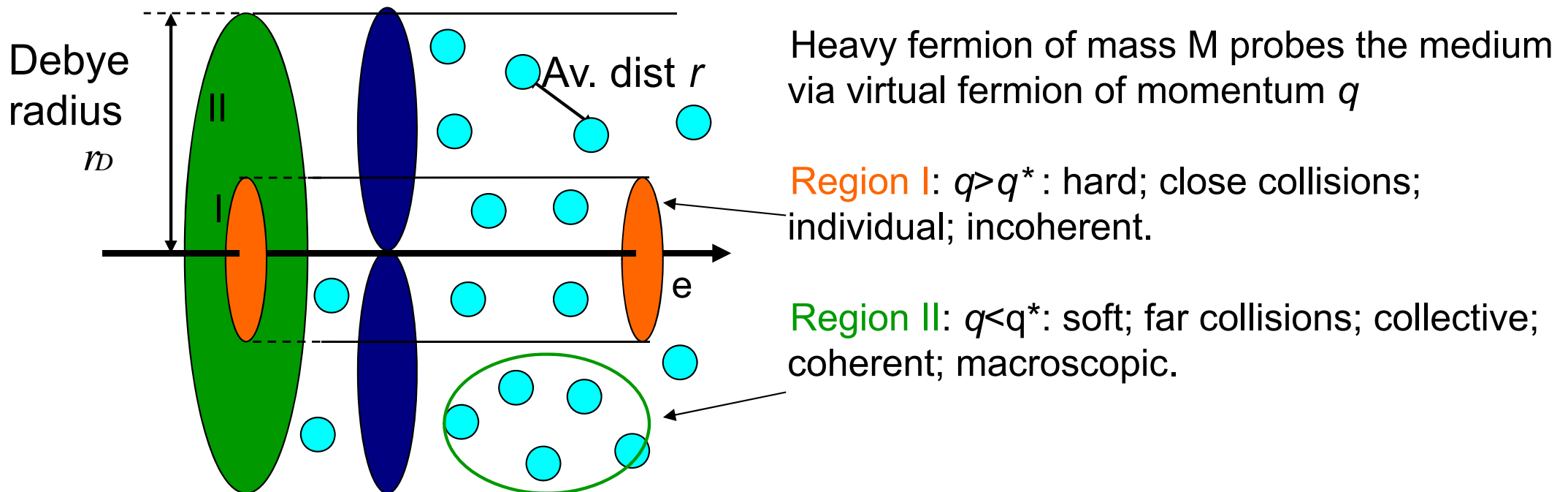
Educated: Calibrating on HTL...  
*permits to fix the effective mass  $\mu$*

# Heavy fermion Energy loss in a relativistic plasma

## Braaten – Yuan scheme

Relying on the smallness of the coupling constant

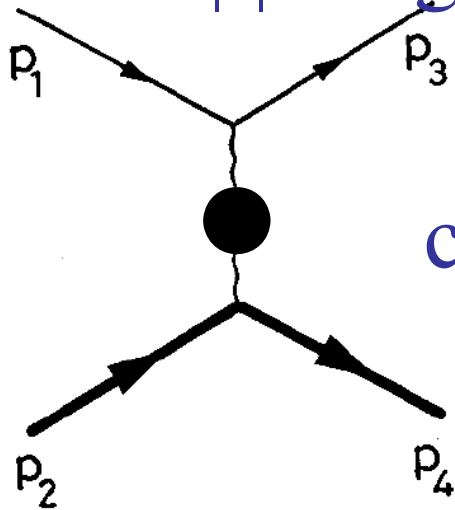
$$\frac{1}{M} \ll r = \frac{1}{T} \ll \frac{1}{q^*} \ll r_D \approx \frac{1}{eT} \ll \lambda \approx \frac{1}{e^2 T}$$



# Braaten-Thoma:

(Peshier – Peigné)

Low  $|t|$ : large distances



HTL:  
collective  
modes

$$G_{\mu\nu}(Q) = \frac{-\delta_{\mu 0}\delta_{\nu 0}}{q^2 + \Pi_{00}} + \frac{\delta_{ij} - \hat{q}_i\hat{q}_j}{q^2 - \omega^2 + \Pi_T}$$

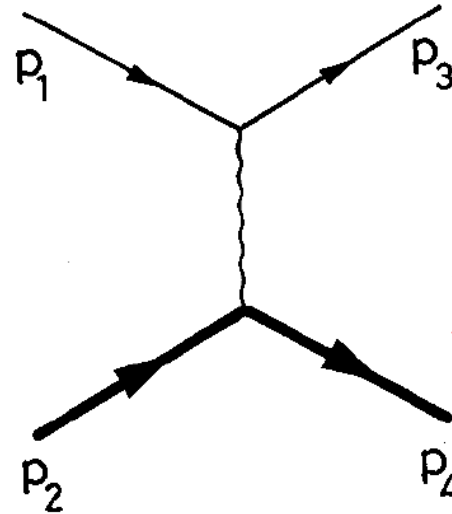
$$\frac{dE_{soft}}{dx} = \frac{2}{3} \alpha m_D^2 \ln\left(\frac{\sqrt{t^*}}{m_D/\sqrt{3}}\right) + \dots$$

**SUM:**  $\frac{dE}{dx} = \frac{2}{3} \alpha m_D^2 \ln\left(\frac{\sqrt{ET}}{m_D/\sqrt{3}}\right)$

HTL: convergent kinetic  
(matching 2 regions)

$|t^*|$

Large  $|t|$ : close coll.



Bare  
propagator

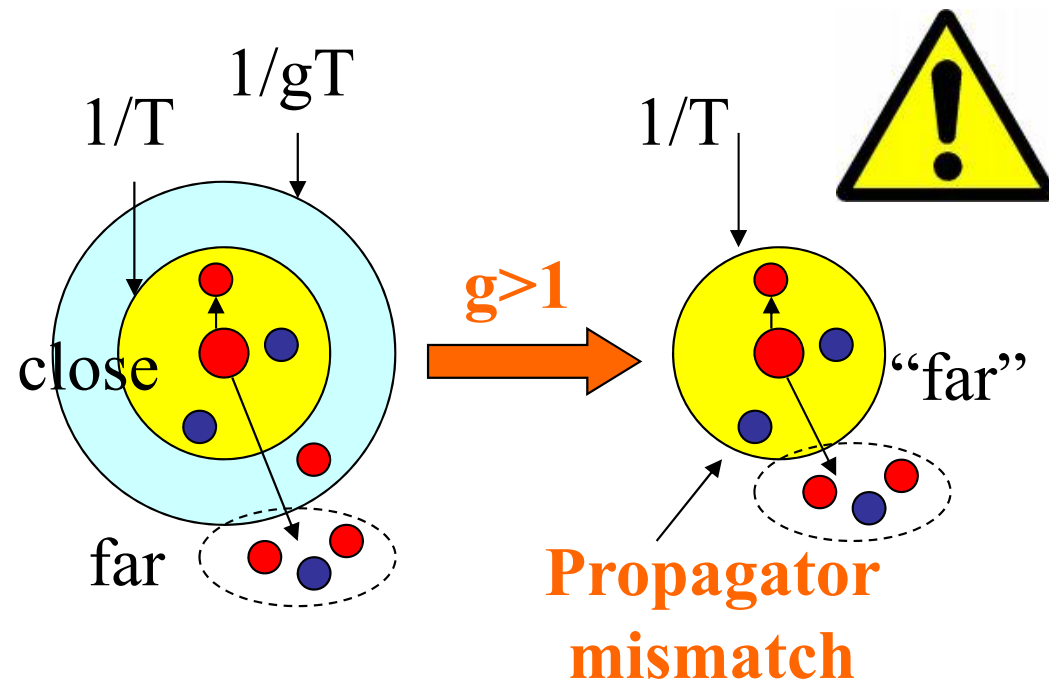
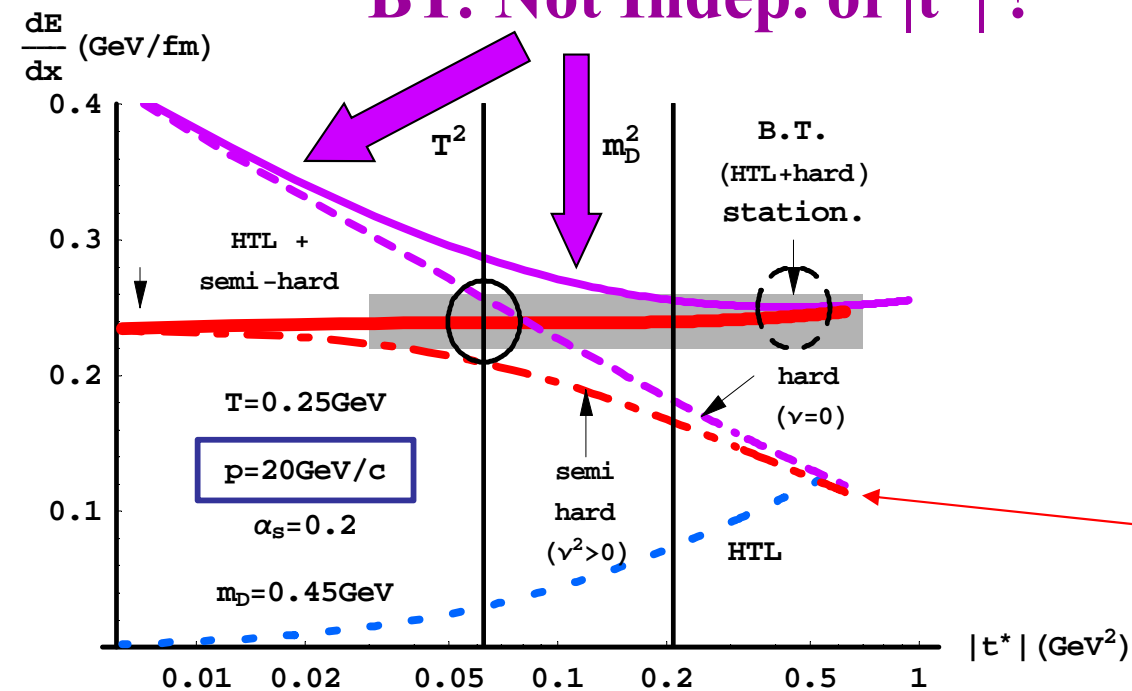
$$G_{\mu\nu}(Q) = \frac{-\delta_{\mu\nu}}{q^2 - \omega^2}$$

$$\frac{dE_{hard}}{dx} = \frac{2}{3} \alpha m_D^2 \ln\left(\frac{\sqrt{ET}}{\sqrt{t^*}}\right) + \dots$$

Indep. of  $|t^*|$  !  
(provided  $g^2 T^2 \ll |t^*| \ll T^2$ )

In QGP:  $g^2 T^2 > T^2$  !!!

BT: Not Indep. of  $|t^*|$  !



Our solution: Introduce a **semi-hard propagator** --  $1/(t-v^2)$  -- for  $|t| > |t^*|$  to attenuate the discontinuities at  $t^*$  in BT approach.

**Prescription:**  $v^2$  in the semi-hard prop. is *chosen* such that the resulting E loss is **maximally  $|t^*|$ -independent**.

This allows a matching at a natural value of  $|t^*| \approx T$ ... Not an increase wrt Braaten-Thoma



# Model C: optimal $\mu^2$

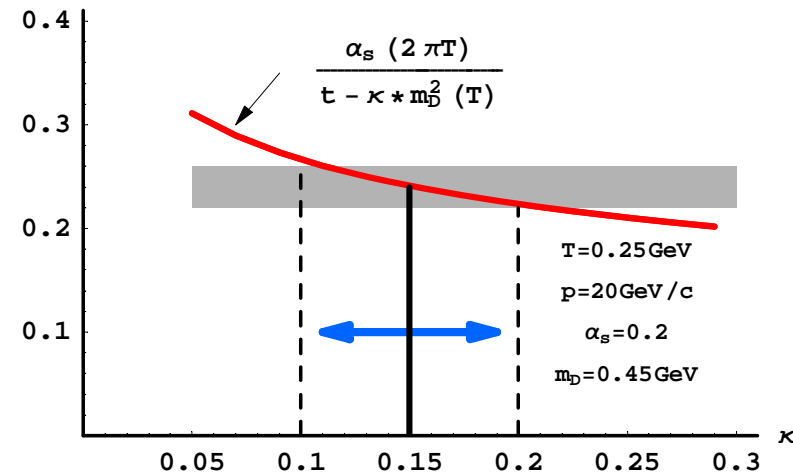
THEN: Optimal choice of  $\mu$  in our OBE model:  $\frac{dE}{dx}$  (GeV/fm)

$$\frac{\alpha_s(2\pi T)}{t - \mu^2}$$

$$\mu^2(T) = \kappa m_D^2(T)$$

With  $\kappa \approx 0.15$

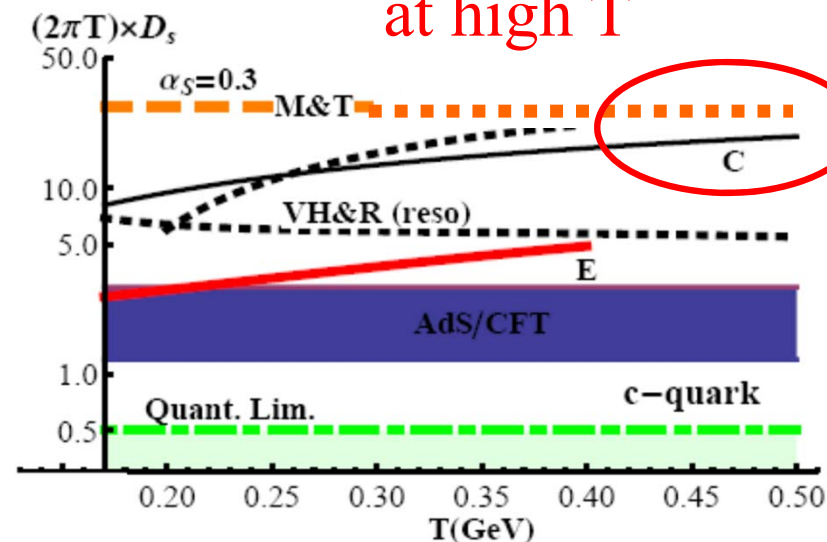
with  $m_D^2 = 4\pi\alpha_s(2\pi T)(1+3/6) \times T^2$



$\frac{dE_{coll}(c)}{dx}$  ... factor 2 increase w.r.t. mod B (not enough to explain  $R_{AA}$ )

T(MeV) \ p(GeV/c)	10	20
200	0.36 (0.18)	0.49 (0.27)
400	0.70 (0.35)	0.98 (0.54)

Convergence with “pQCD” at high T



# Refined: *running coupling constant*

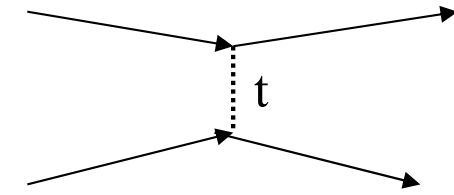
Motivation: Even a fast parton with the largest momentum  $P$  will undergo collisions with moderate  $q$  exchange and large  $\alpha_s(Q^2)$ . The running aspect of the coupling constant has been “forgotten/neglected” in most of approaches

Open question: long range behaviour and renormalisation at finite temperature

# A Peshier: $\alpha_S$ not fixed at the right scale

Running of  $\alpha_S$  (Peshier 06) in collisional E loss

Usually 
$$\frac{dE_j}{dx} = \sum_s \int_{k^3} \rho_s(k) \Phi \int dt \frac{d\sigma_{js}}{dt} \omega$$



with 
$$\Phi \int_{t_1}^{t_2} dt \frac{d\sigma_{js}}{dt} \omega = \frac{\pi C_{js} \alpha^2}{-k} \int_{t_1}^{t_2} \frac{dt}{t} = \frac{\pi C_{js} \alpha^2}{k} \ln \frac{t_1}{t_2}$$
 and  $\alpha_S(2\pi T)$

Doing it more cautiously

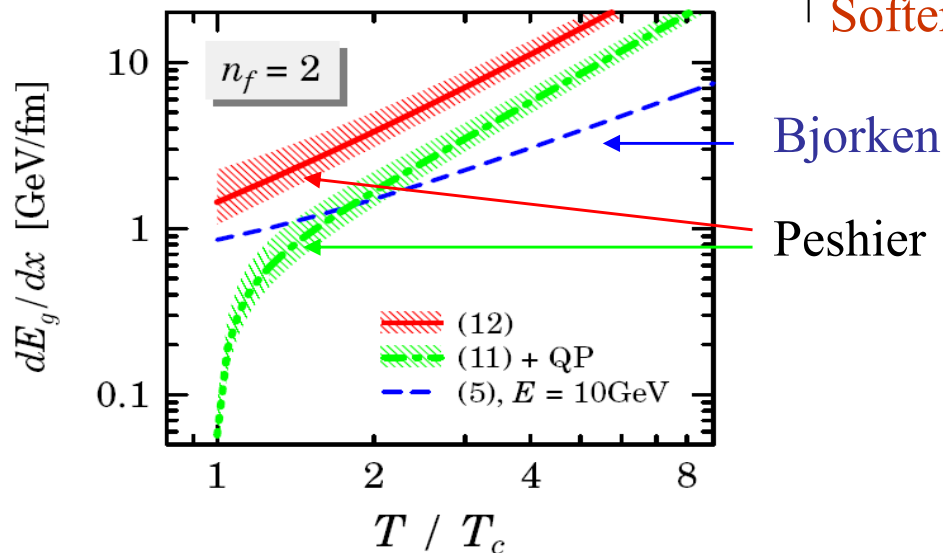
$$\Phi \int_{t_1}^{t_2} dt \frac{d\sigma_{js}}{dt} \omega = -\frac{\pi C_{js}}{k b_0^2} \int_{t_1}^{t_2} \frac{dt}{t \ln^2(|t|/\Lambda^2)}$$

← Dominated by the soft scale

$$= \frac{\pi C_{js}}{k b_0^2} \frac{1}{\ln(|t|/\Lambda^2)} \Big|_{t_1}^{t_2} = \frac{\pi C_{js}}{k b_0} [\alpha(\mu^2) - \alpha(|t_1|)]$$

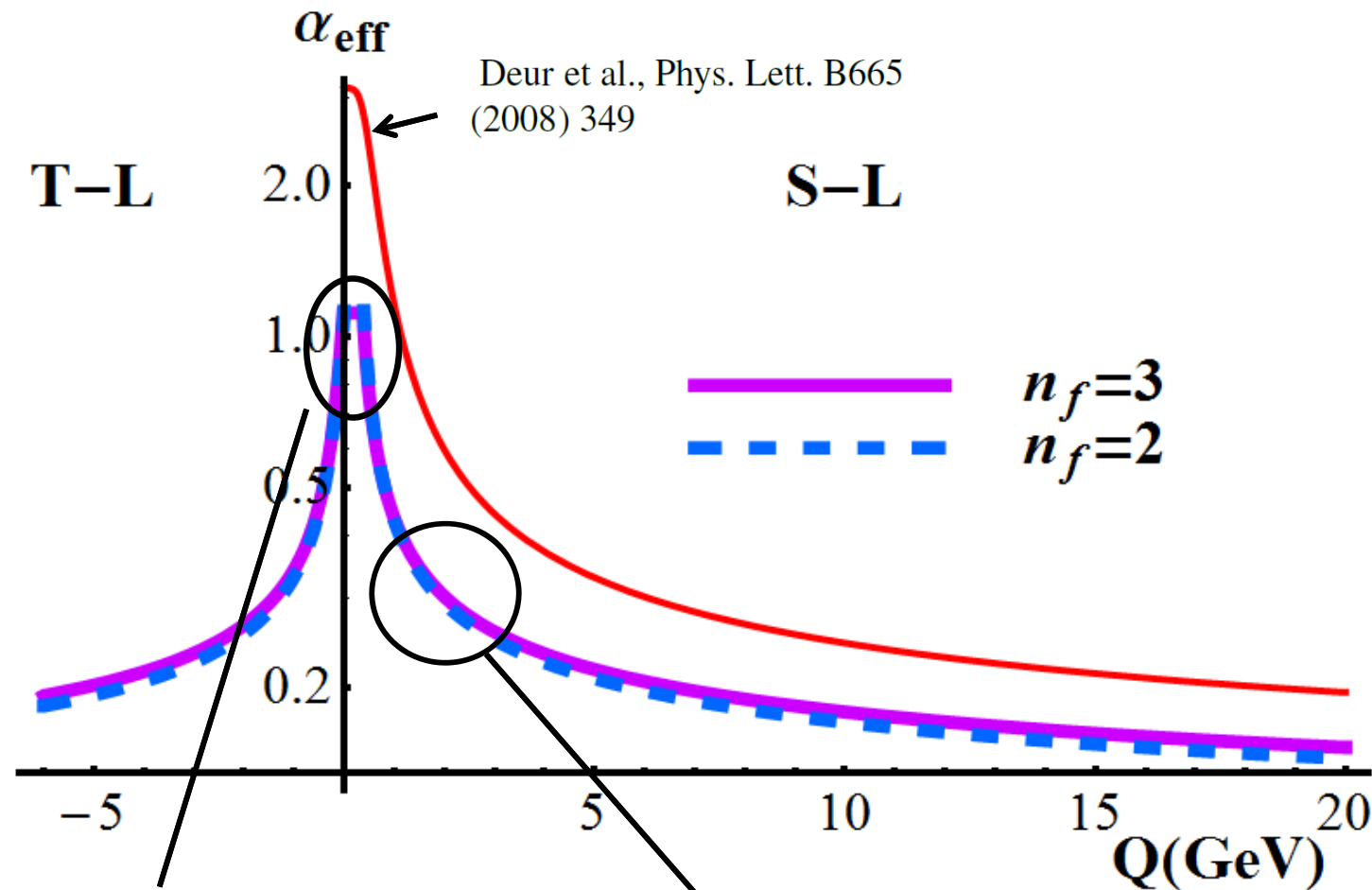
← No log(E) increase. UV conv. for  $t_1 \rightarrow \infty$

Softer scale  $\Rightarrow$  larger E loss !!!



"In fact,  $\sigma$  with running coupling ... an order of magnitude larger than expected from the widely used expression  $\sigma_{\alpha \text{ fix}} \propto \alpha^2(Q^2 T) / \mu^2$ . Thus, the present approach gives a consistent and simple explanation of phenomenologically inferred large cross sections found in transport models."

# running $\alpha_s$



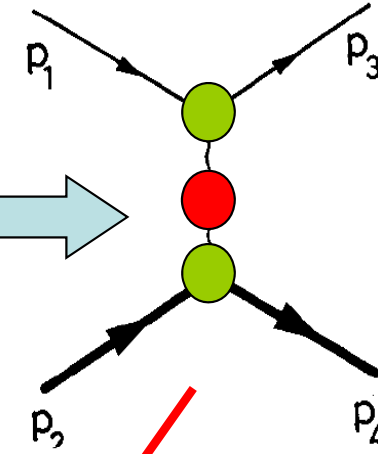
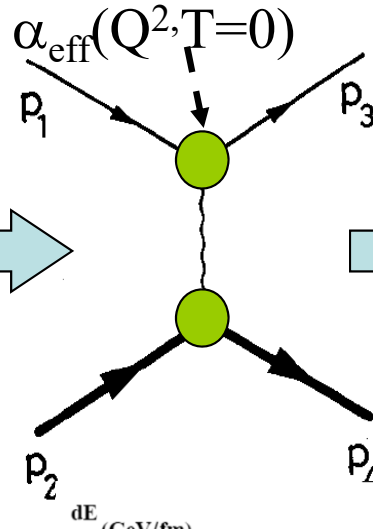
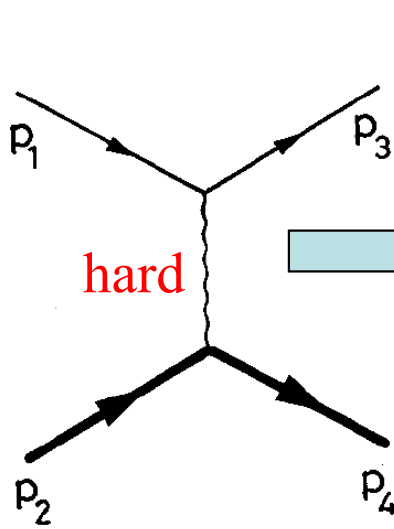
IR safe. The detailed form very close to  $Q^2=0$  is not important does not contribute to the energy loss

Large values for intermediate momentum-transfer => larger cross section

**Of course, still a lot of uncertainties in the choice of this essential quantity !!!**

# $\mu$ -local-model: medium effects at finite T in t-channel

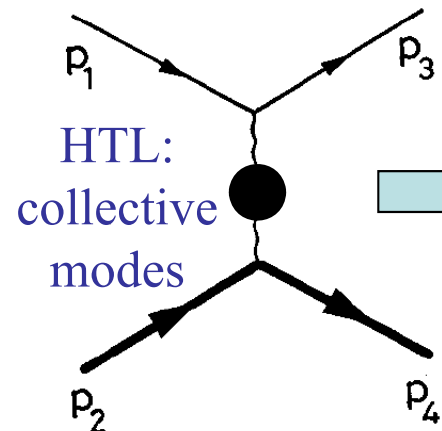
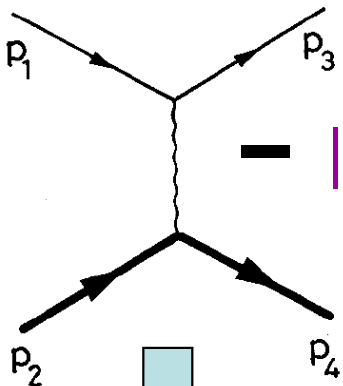
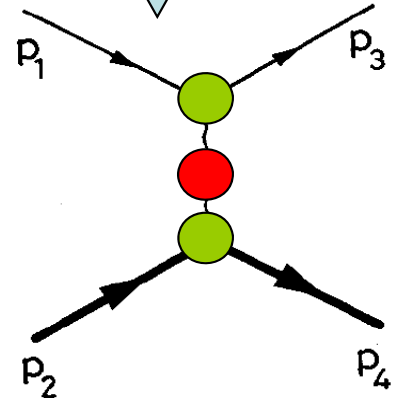
Large  $|t|$



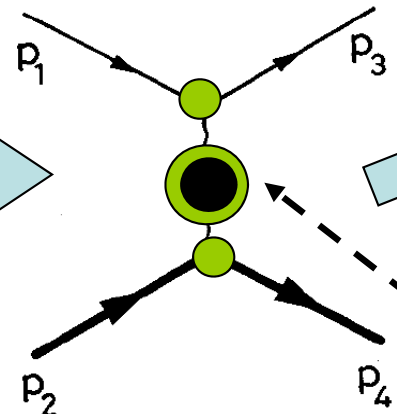
Semi-hard

$$\frac{\alpha_{\text{eff}}(t)}{t - \lambda m_D^2(T, t)}$$

$\lambda=0.11$

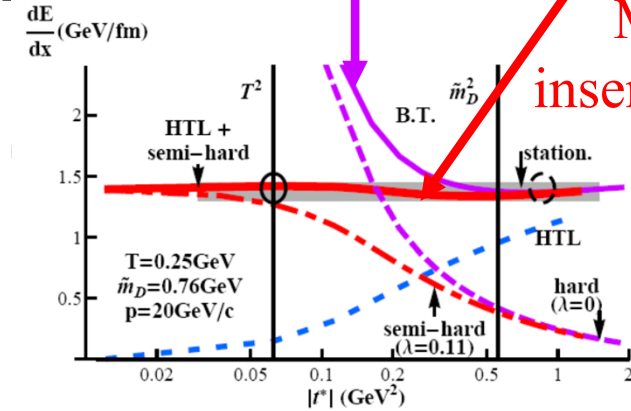


Low  $|t|$



Bona Fide running HTL:  
 $\alpha_s \rightarrow \alpha_s(t)$  in  $\Pi_L$  and  $\Pi_T$

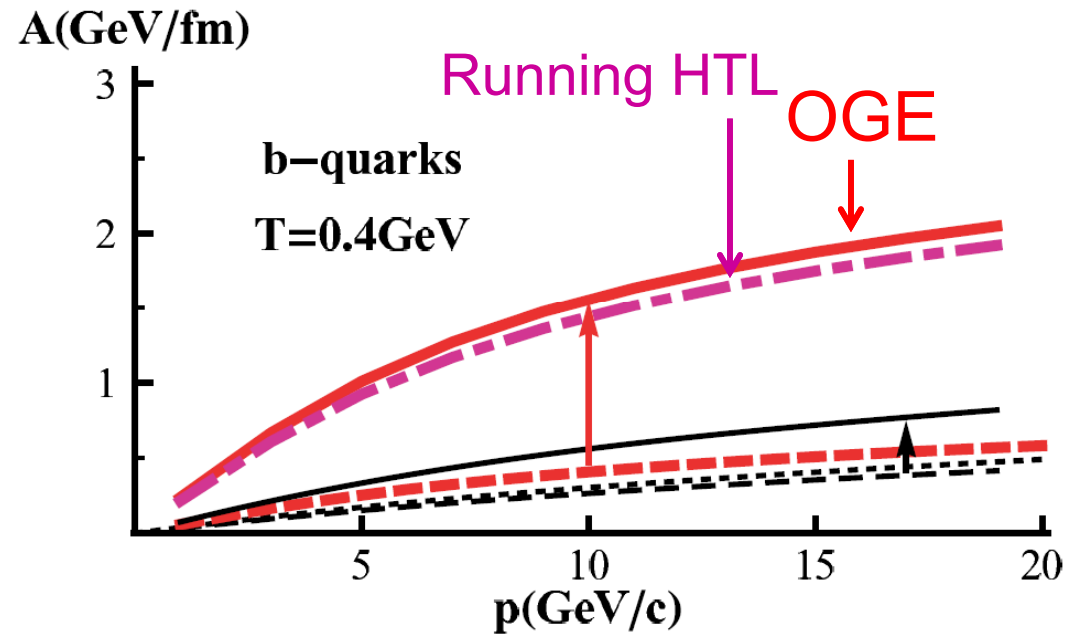
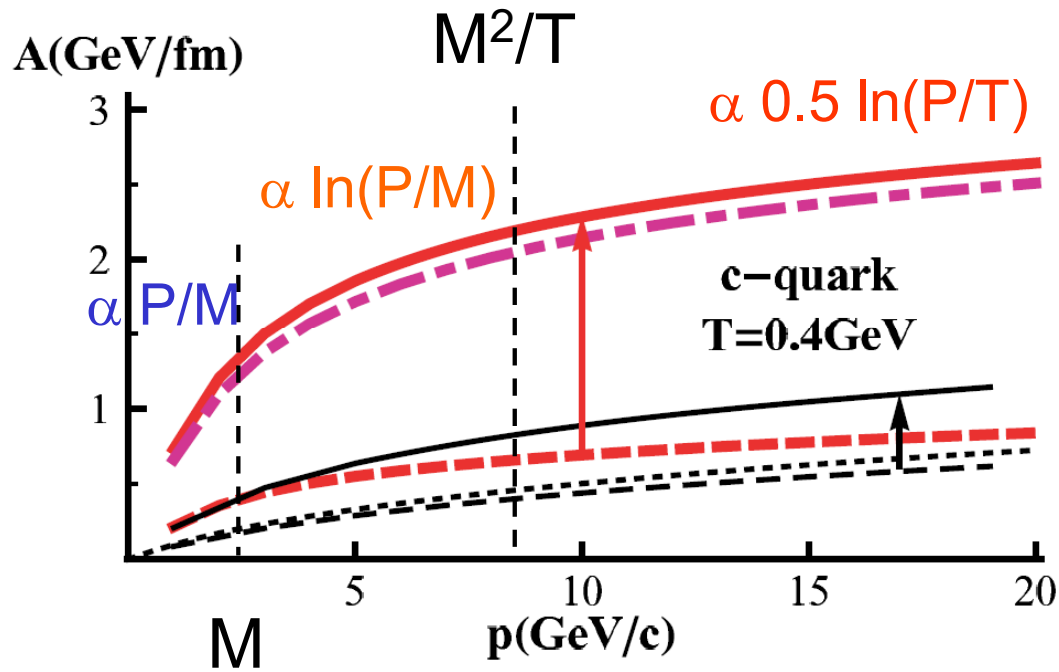
BT



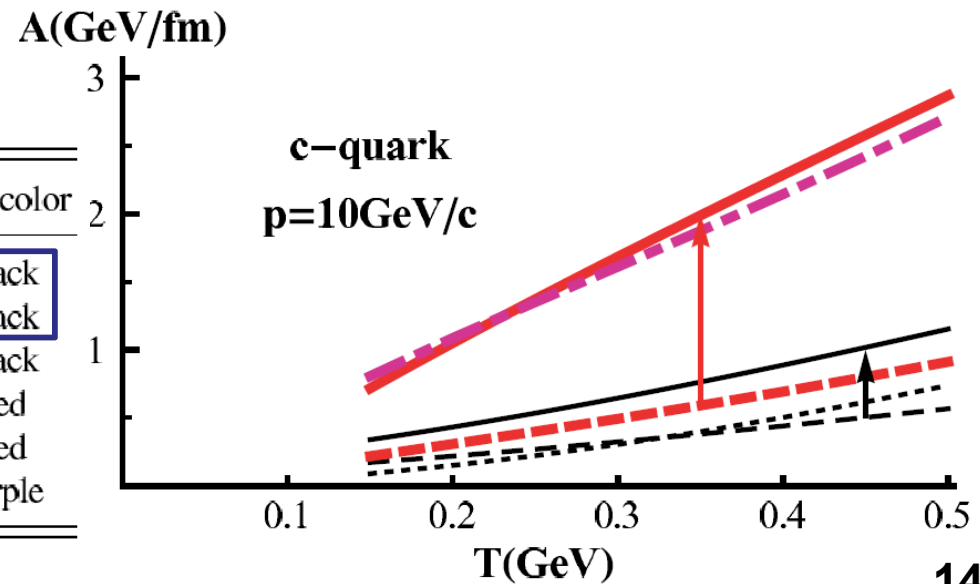
OGE with effective  
polarisation  
 $\mu^2(T)=0.2 m_{D\text{self}}^2(T)$

$$m_{D\text{self}}^2(T) = (1+n_f/6) 4\pi\alpha_{\text{eff}}(m_{D\text{self}}^2) T^2$$

# Drag coefficient $A$ ( $d\langle p \rangle/dt$ )



At large  $p$ : moderate mass dependence

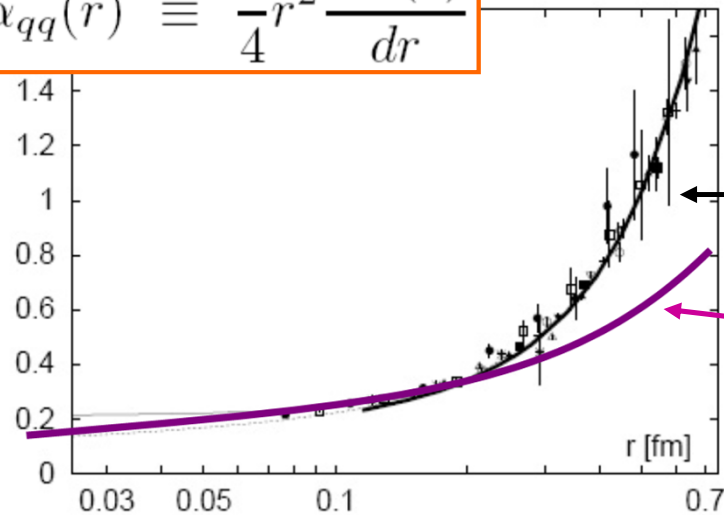


	$\alpha_S$	$\mu^2$	Line form	Line color
A	0.3	$m_D^2$	Dotted thin	Black
B	$\alpha_S(2\pi T)$	$m_D^2$	Dashed thin	Black
C	$\alpha_S(2\pi T)$	$0.15m_D^2$	Full thin	Black
D	Running, Eq. (17)	$\tilde{m}_D^2$	Dashed bold	Red
E	Running, Eq. (17)	$0.2\tilde{m}_D^2$	Full bold	Red
F	Running, Eq. (17)	$0.11(6\pi \alpha_{\text{eff}}(t) T^2)$	Dashed dotted bold	Purple

# $\mu$ -local-model: Eff. Running $\alpha_s$ vs lQCD

**T=0**

$$\alpha_{qq}(r) \equiv \frac{3}{4} r^2 \frac{dV(r)}{dr}$$



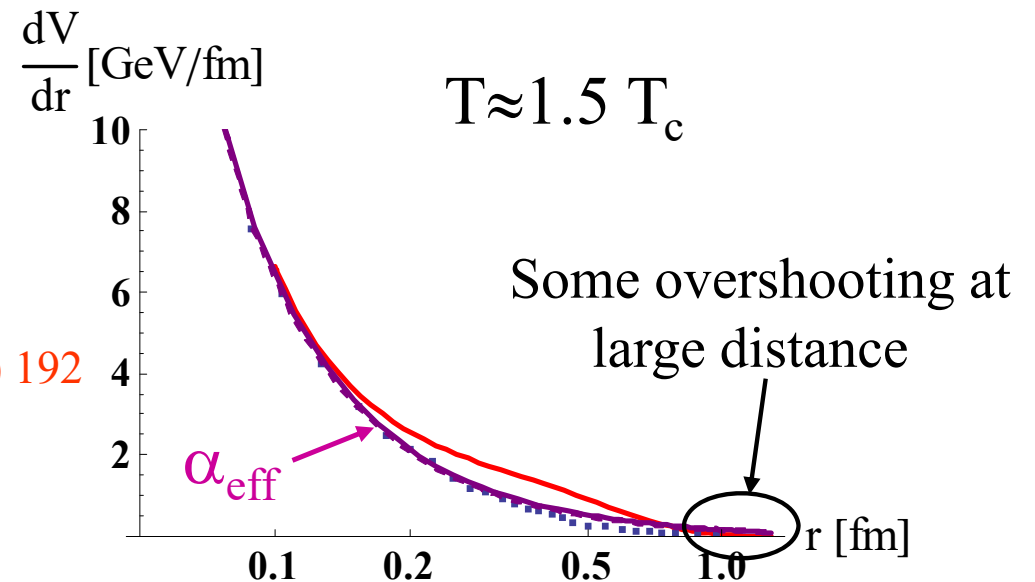
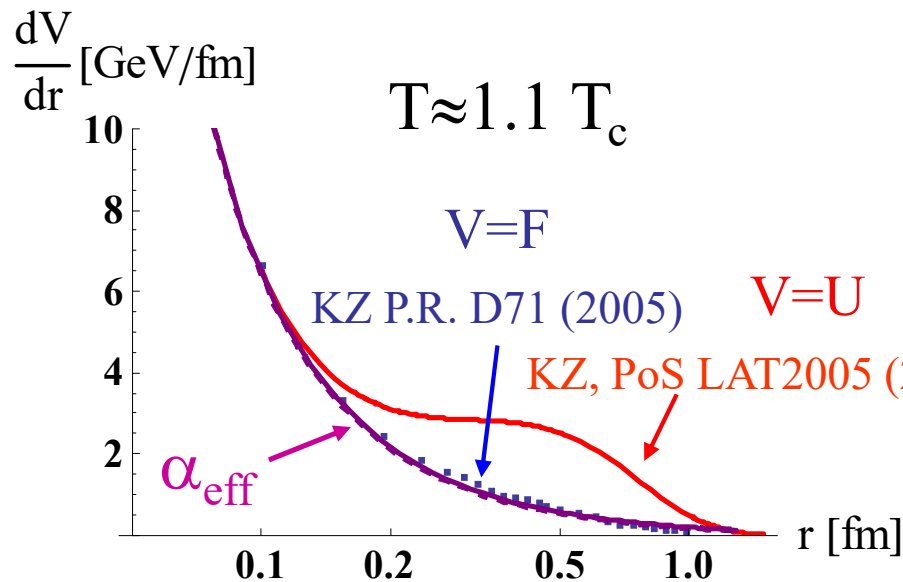
O. Kaczmarek & F. Zantow (KZ) ( $n_f=2$  QCD), P.R.D71 (2005) 114510

Genuine non-pert (string)

optimal  $\mu$ , running  $\alpha_{\text{eff}}$

V: $\omega=0$  sector; dE/dx: finite  $\omega$

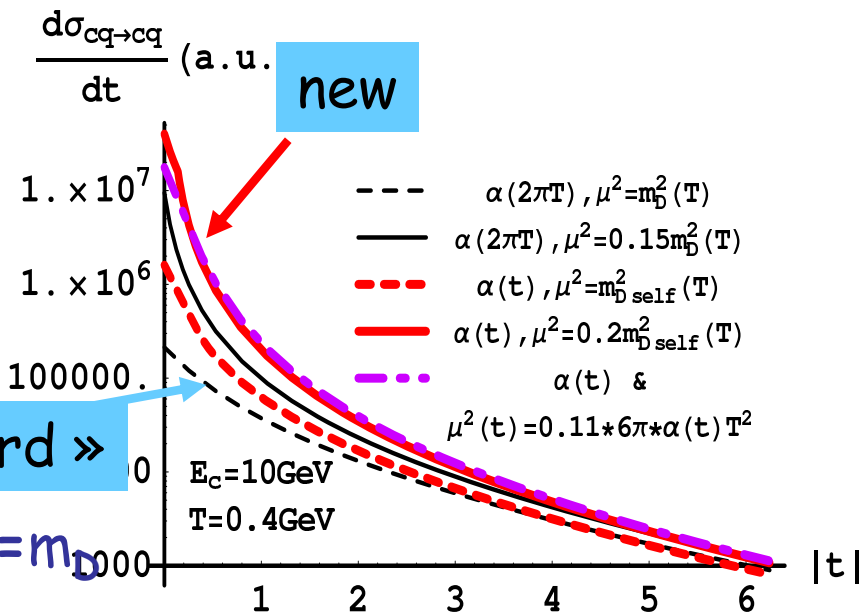
**Finite T**



**Merging at  $\approx 2 T_c$**

# Differential cross sections

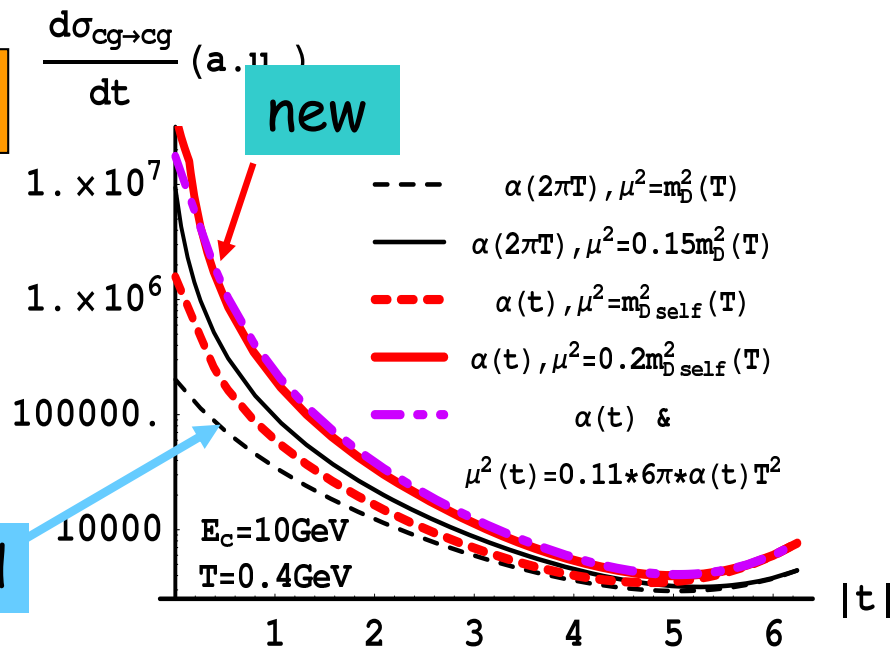
**Qq->Qq**



Large enhancement of both cross sections at small and intermediate  $|t|$

Little change at large  $|t|$

**Qg->Qg**



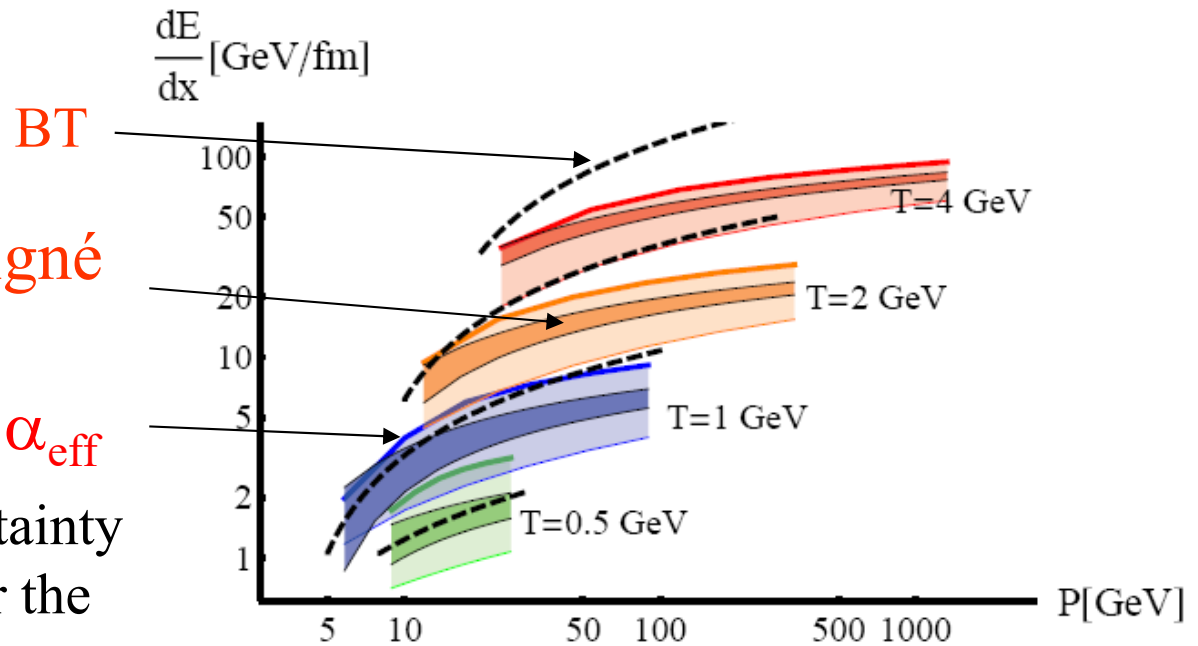


# $\mu$ -local-model: Eff. Running vs fixed $\alpha_s$

Dark bands: Peshier & Peigné  
(2008)

E: optimal  $\mu$ , running  $\alpha_{\text{eff}}$

Light bands: theoretical uncertainty  
related to the prescription for the  
HTL-hard transition



## Conclusions:

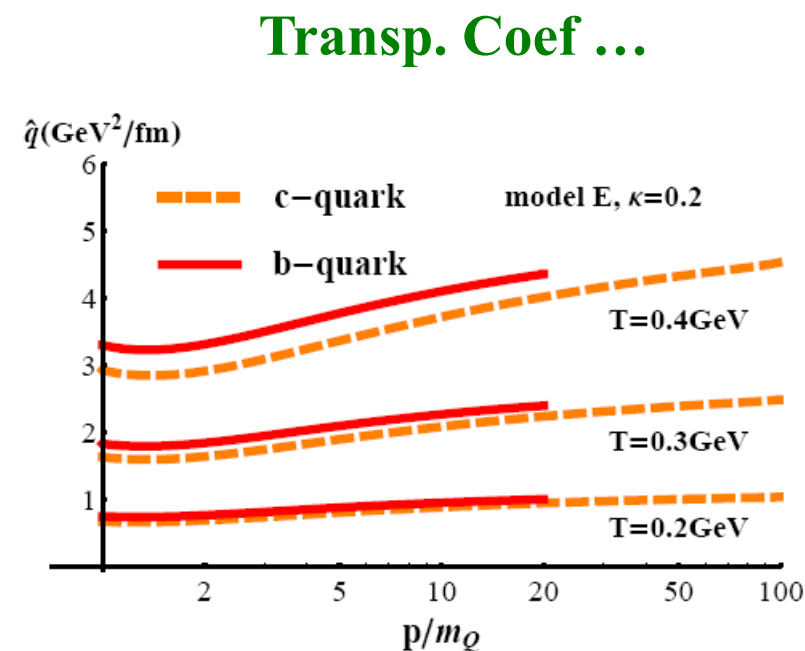
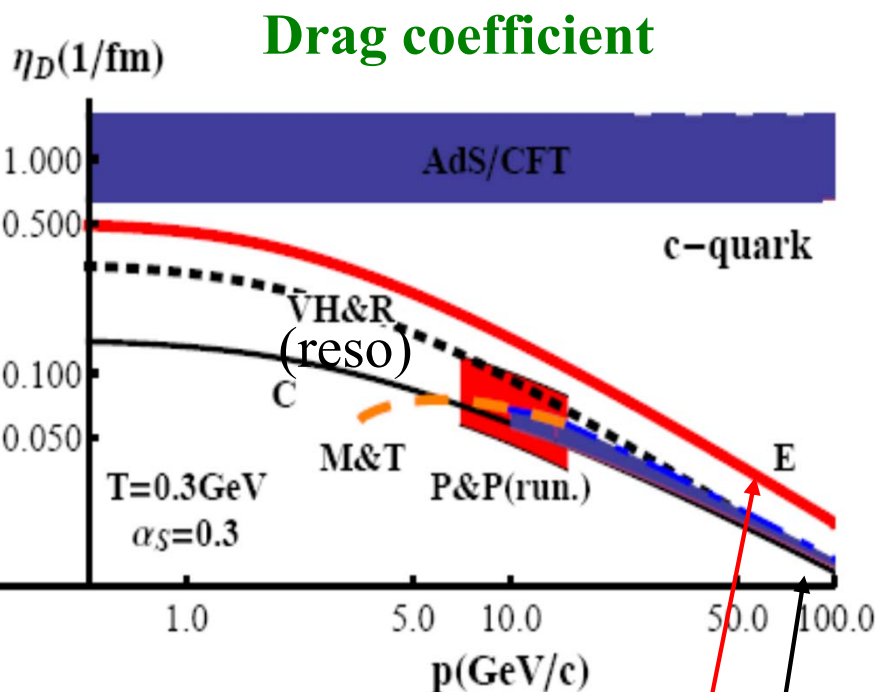
- Good agreement with PP for large T and large P
- Running  $\alpha_s$  is more than a cranking of BT (different shapes and T-dependences)

# Running $\alpha_s$ : some Energy-Loss values

$$\frac{dE_{coll}(c/b)}{dx}$$

T(MeV) \ p(GeV/c)	10	20
200	1 / 0.65	1.2 / 0.9
400	2.1 / 1.4	2.4 / 2

$\approx 10\%$  of HQ energy

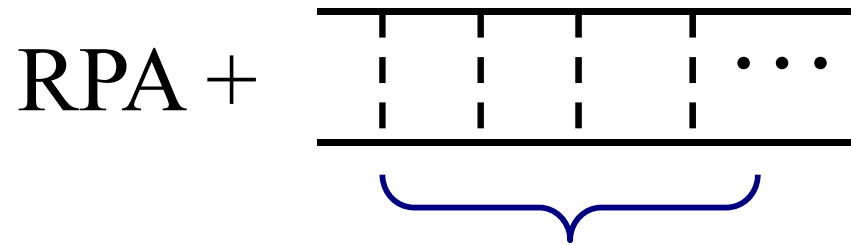


E: optimal  $\mu$ , running  $\alpha_{eff}$   
 C: optimal  $\mu$ ,  $\alpha_s(2\pi T)$

... of expected magnitude to reproduce the data (we “explain” the transp. Coeff. in a rather parameter free approach).

# Several issues

1. Non perturbative aspects (beyond Born). Usually in convergent kinetic:

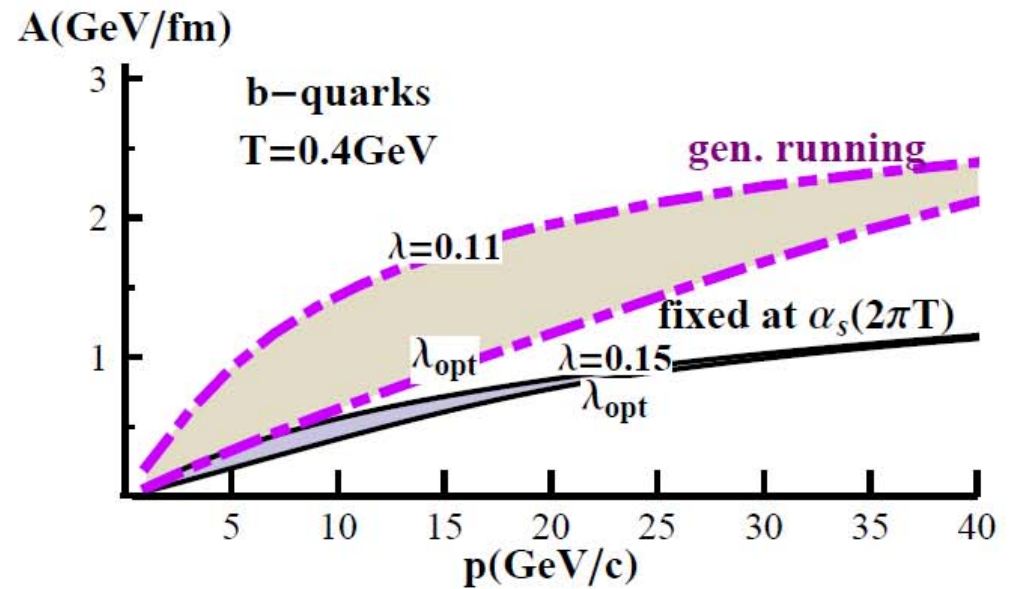
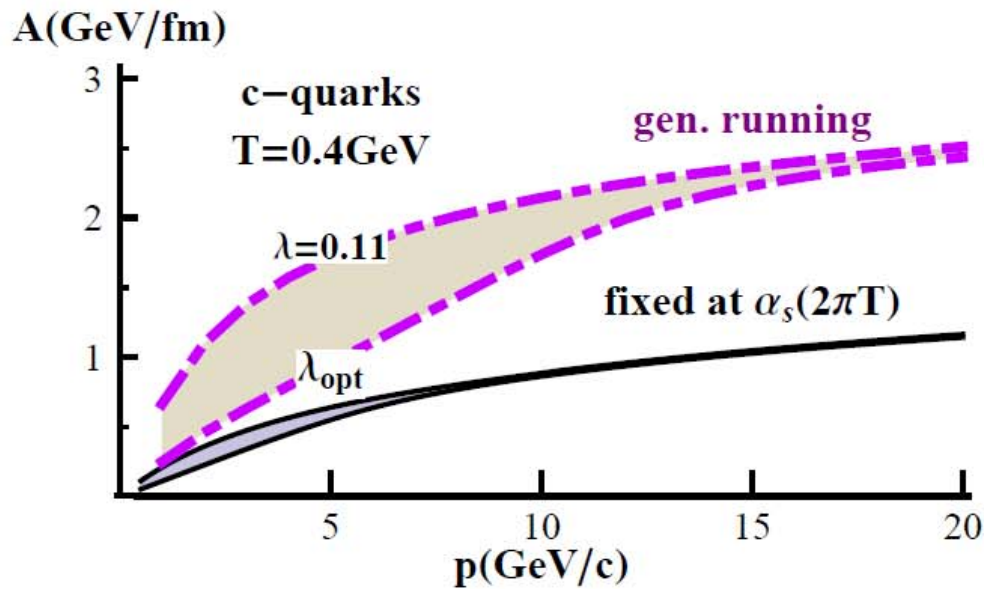
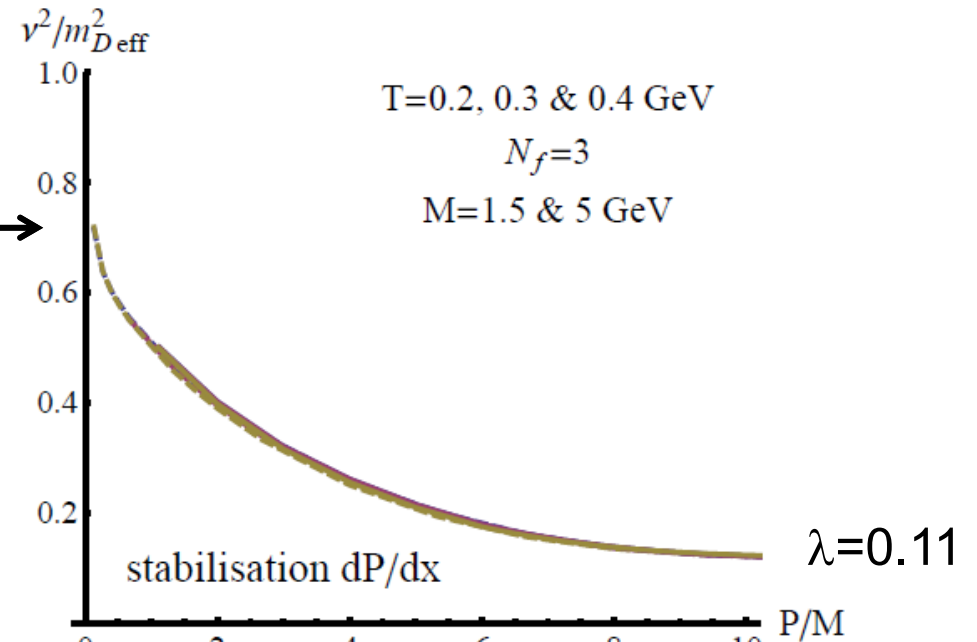


Ladders necessary at short  
distance (large force)

# Several issues

## 2. $\lambda$ at small momentum ?

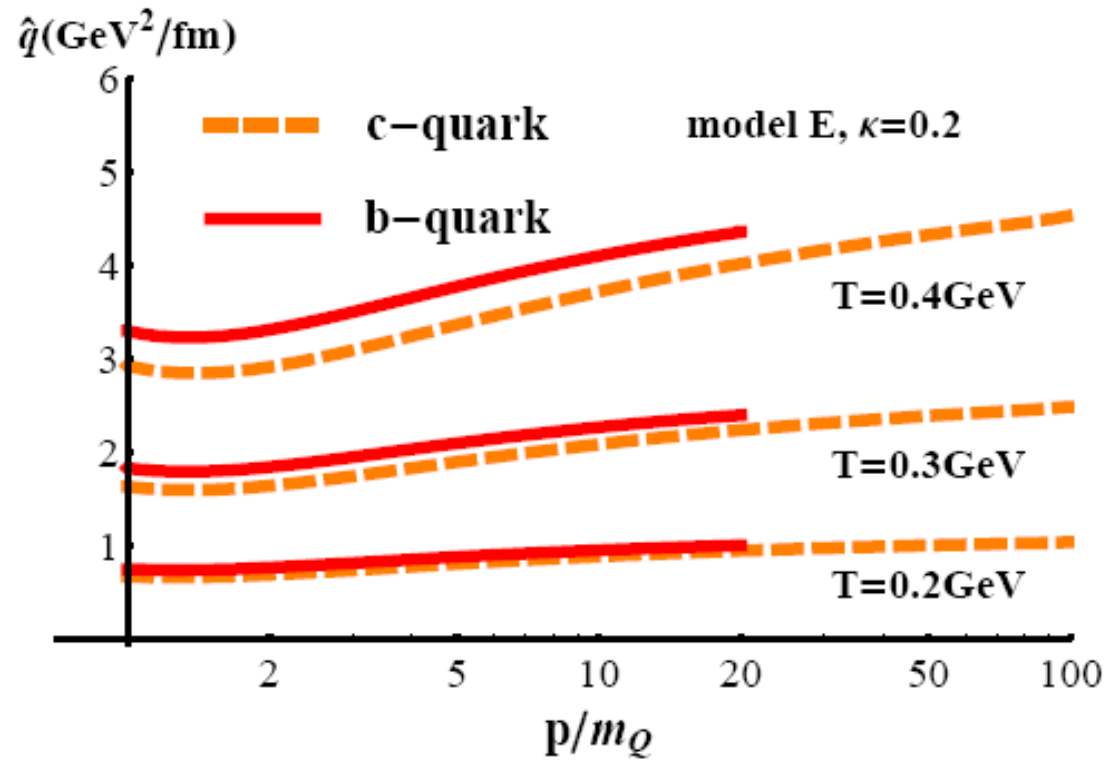
Reduction of the interaction range  $\rightarrow$



## Several issues

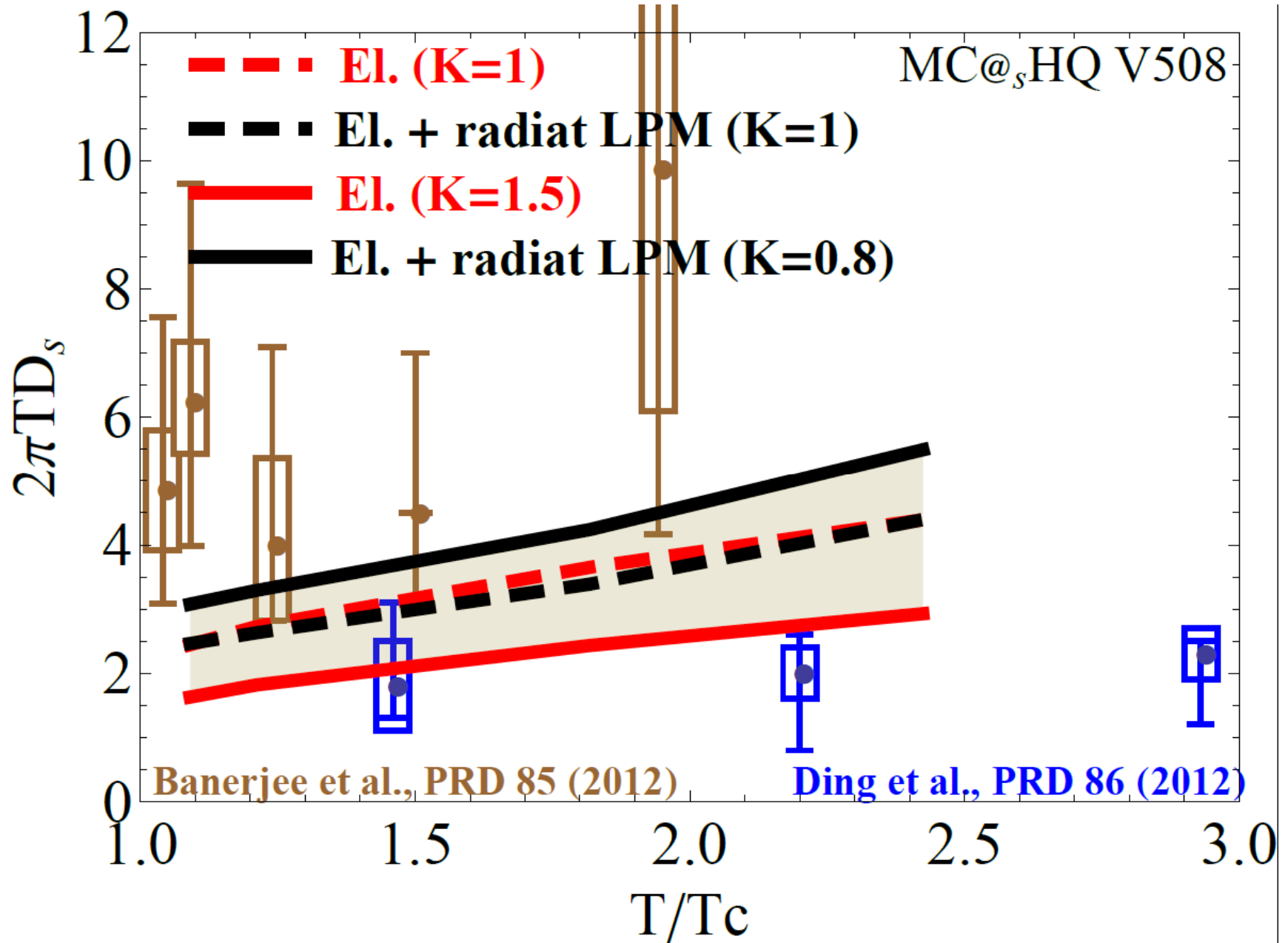
3. How to deal with the genuinely NP part ?

# Transport coefficients (1)



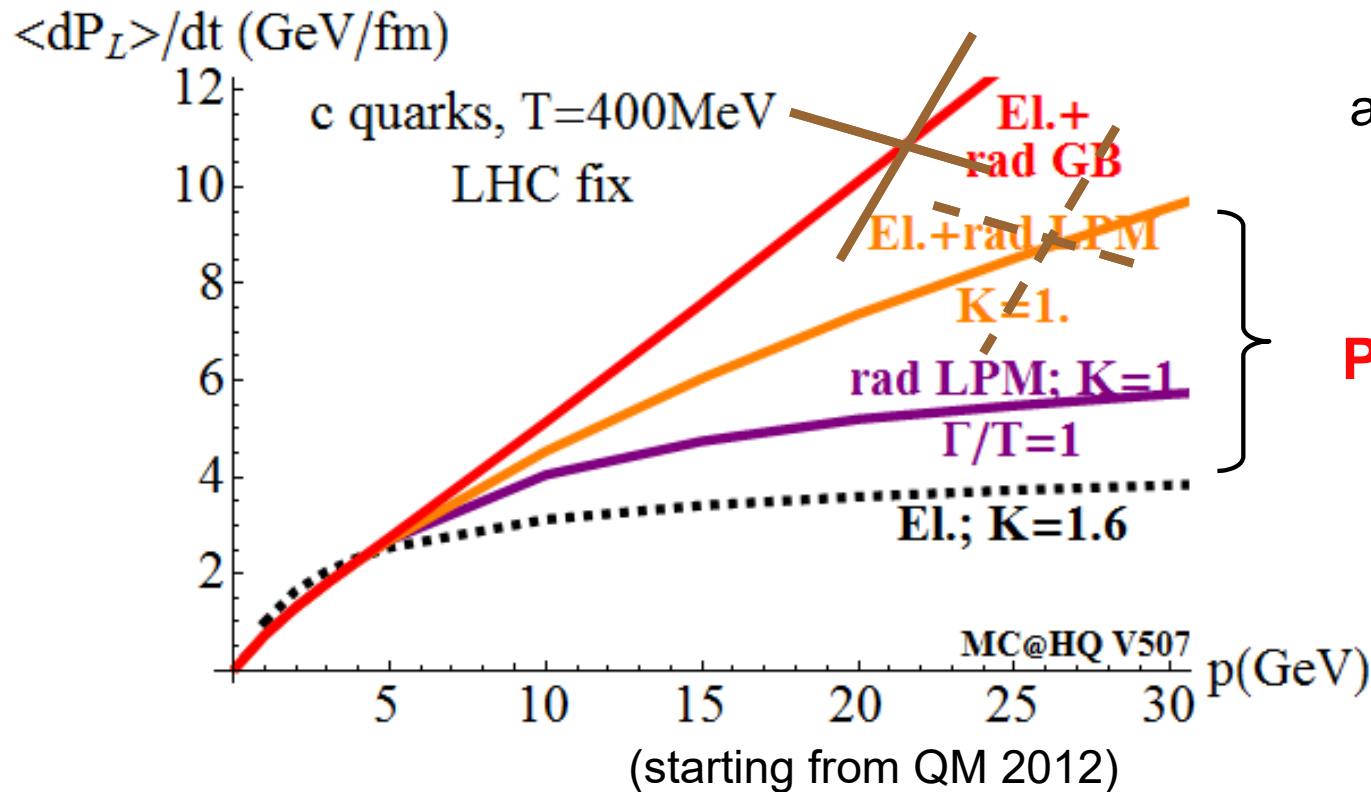
Only the elastic contribution

# Transport coefficients (2)



# Transport coefficients (3)

Gathering all *rescaled* models (*coll. and radiative*) compatible with RHIC  $R_{AA}$ :



the drag coefficient reflects the average momentum loss (per unit time)  $\Rightarrow$  large weight on  $x \sim 1$

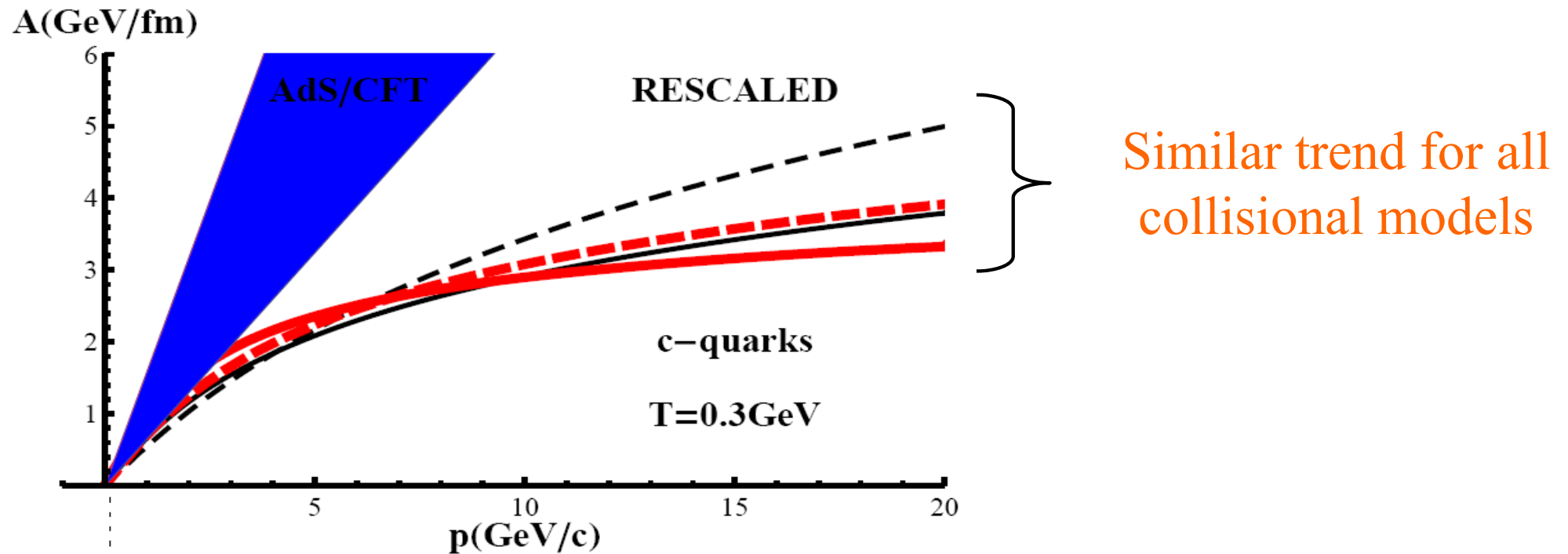
**Present LHC data**

For too large  $p_T$ ,  $L^2$  terms dominate  $\Rightarrow$  transport coefficients are not the relevant objects



# Transport coefficients (4)

Gathering all rescaled models (various prescriptions for  $\mu$  and  $\alpha_s$ ):



AdS/CFT too large to reproduce experimental data ?! Against the conclusion of Akamatsu et al (?)

A16

(E-loss plays a dominant role, but not the only parameter)

## Diapositive 25

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**A16**

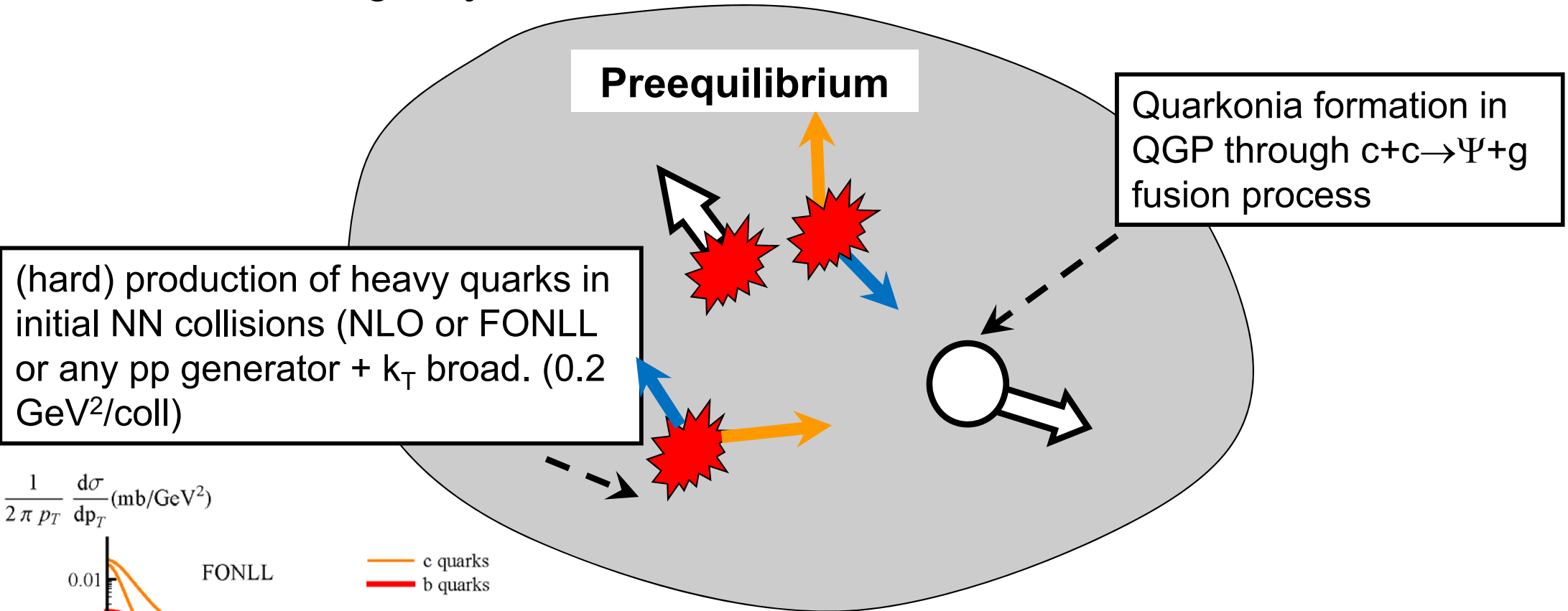
comparer avec hirano et al qui parviendraient à reproduire le RAA

Administrateur; 19/07/2009

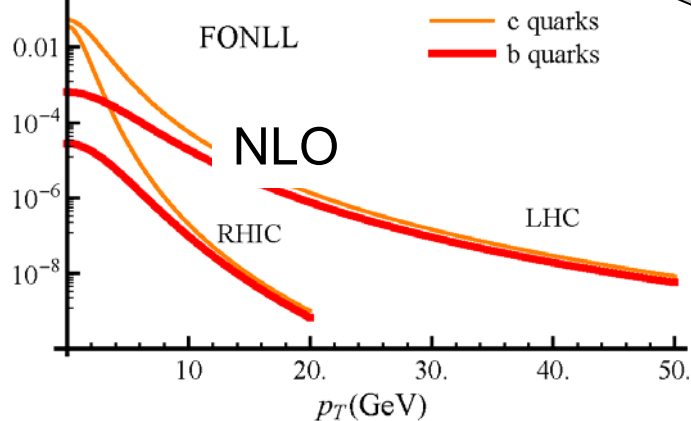
# The Monte Carlo @ Heavy Quark Generator

No force on HQ before thermalization of QGP (0.6 fm/c)

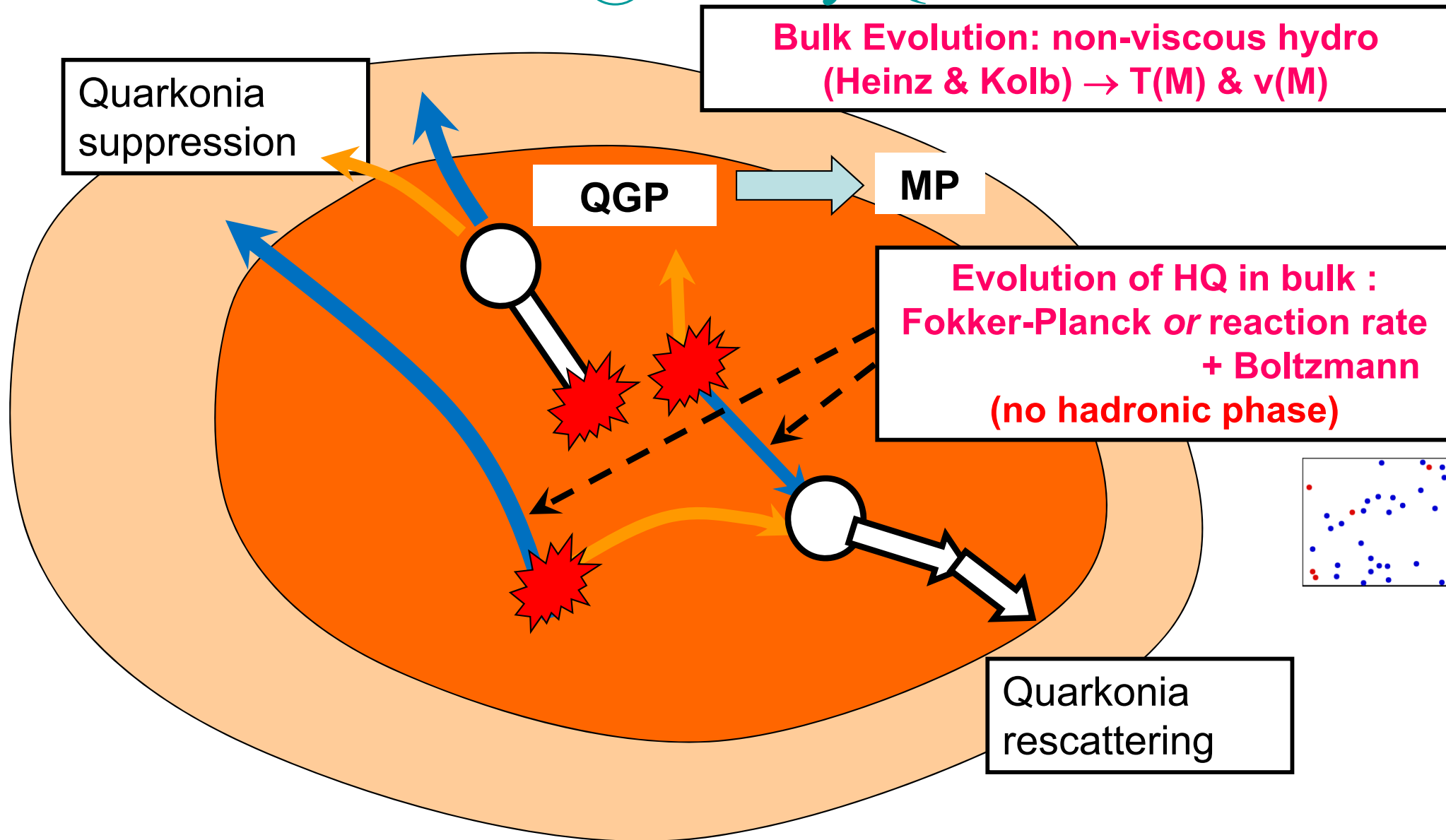
Evolution according to Bjorken time



$$\frac{1}{2\pi p_T} \frac{d\sigma}{dp_T} (\text{mb/GeV}^2)$$



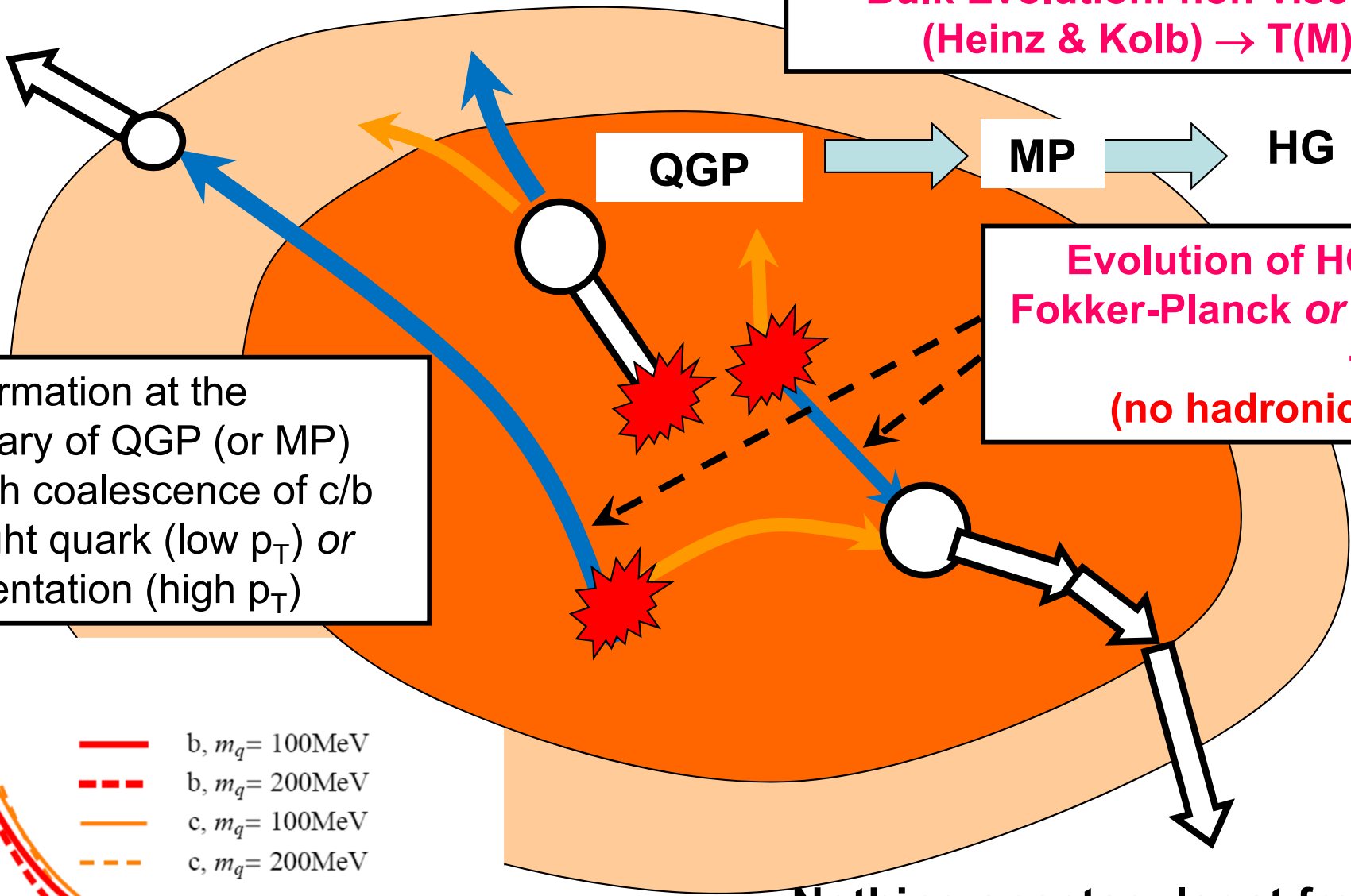
# The Monte Carlo @ Heavy Quark Generator



Recently : coupling to EPOS2 (3) instead of KH

# The Monte Carlo @ Heavy Quark Generator

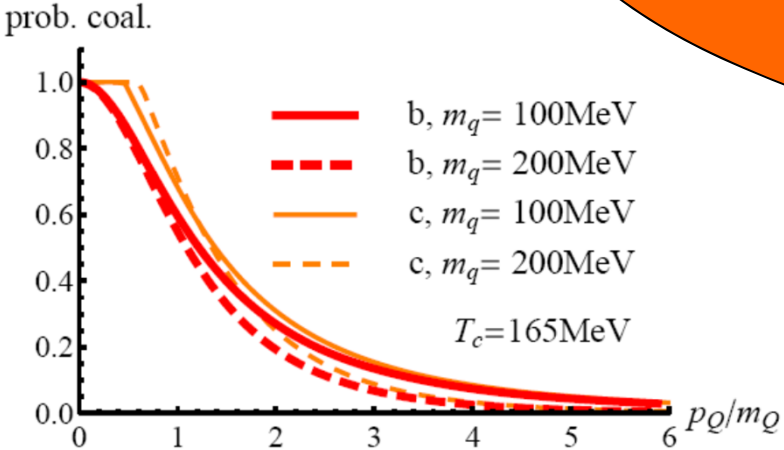
**Bulk Evolution: non-viscous hydro (Heinz & Kolb) →  $T(M)$  &  $v(M)$**



**Evolution of HQ in bulk : Fokker-Planck or reaction rate + Boltzmann (no hadronic phase)**

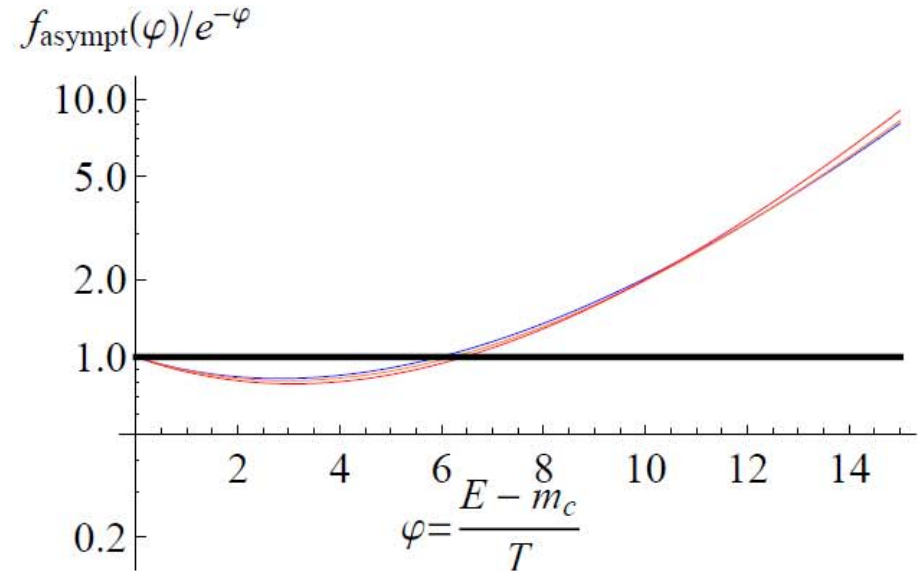
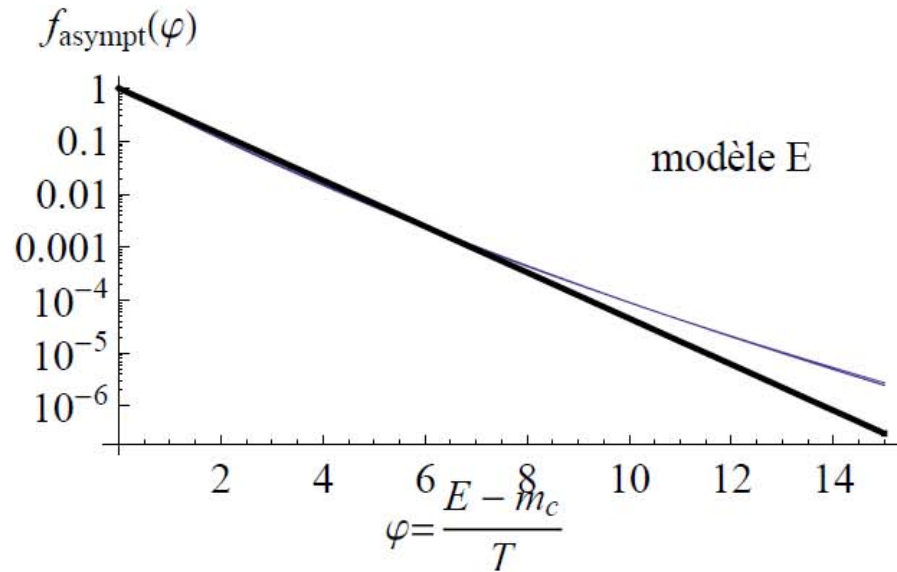
**D/B formation at the boundary of QGP (or MP) through coalescence of c/b and light quark (low  $p_T$ ) or fragmentation (high  $p_T$ )**

**Nothing spectacular at freeze-out (quarkonia are white objects already)**

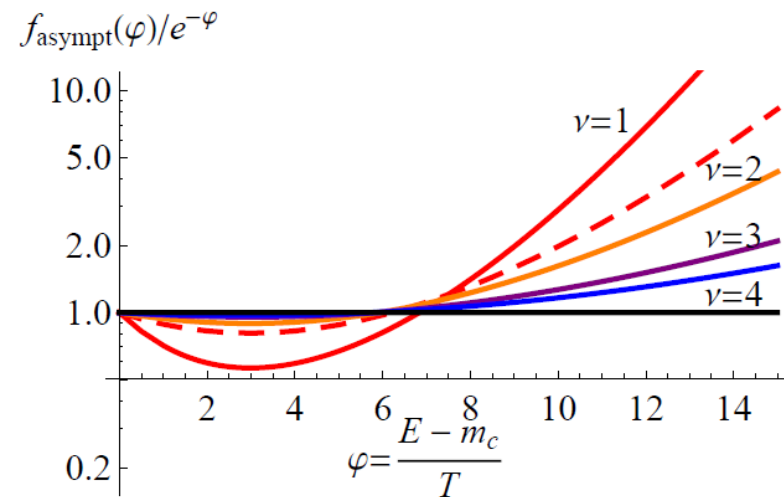


# Boltzmann vs Langevin

Deviation from Einstein relation with native coefficients



$$|\mathcal{M}_{\text{grazing}}(s, t, \mu; \nu)|^2 = \frac{(s - m^2)^2 \mu^{4(\nu-1)}}{(\mu^2 - t)^{2\nu}}$$

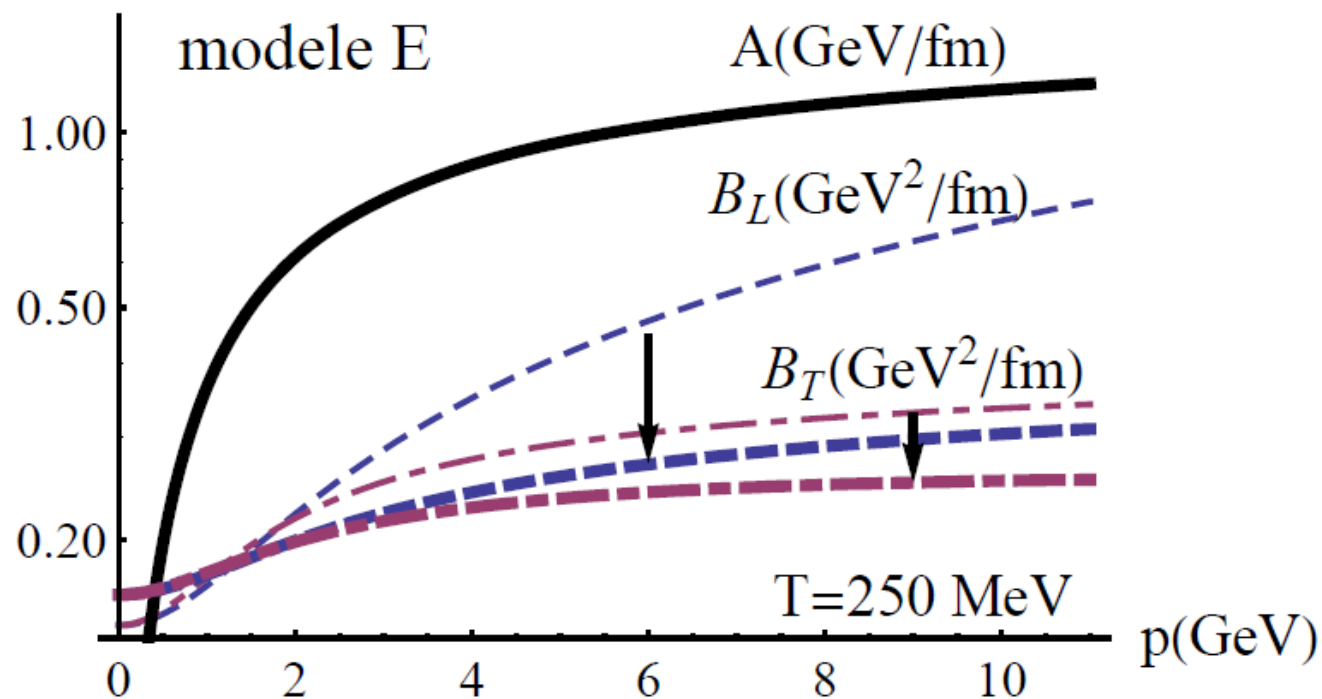


# Boltzmann vs Langevin

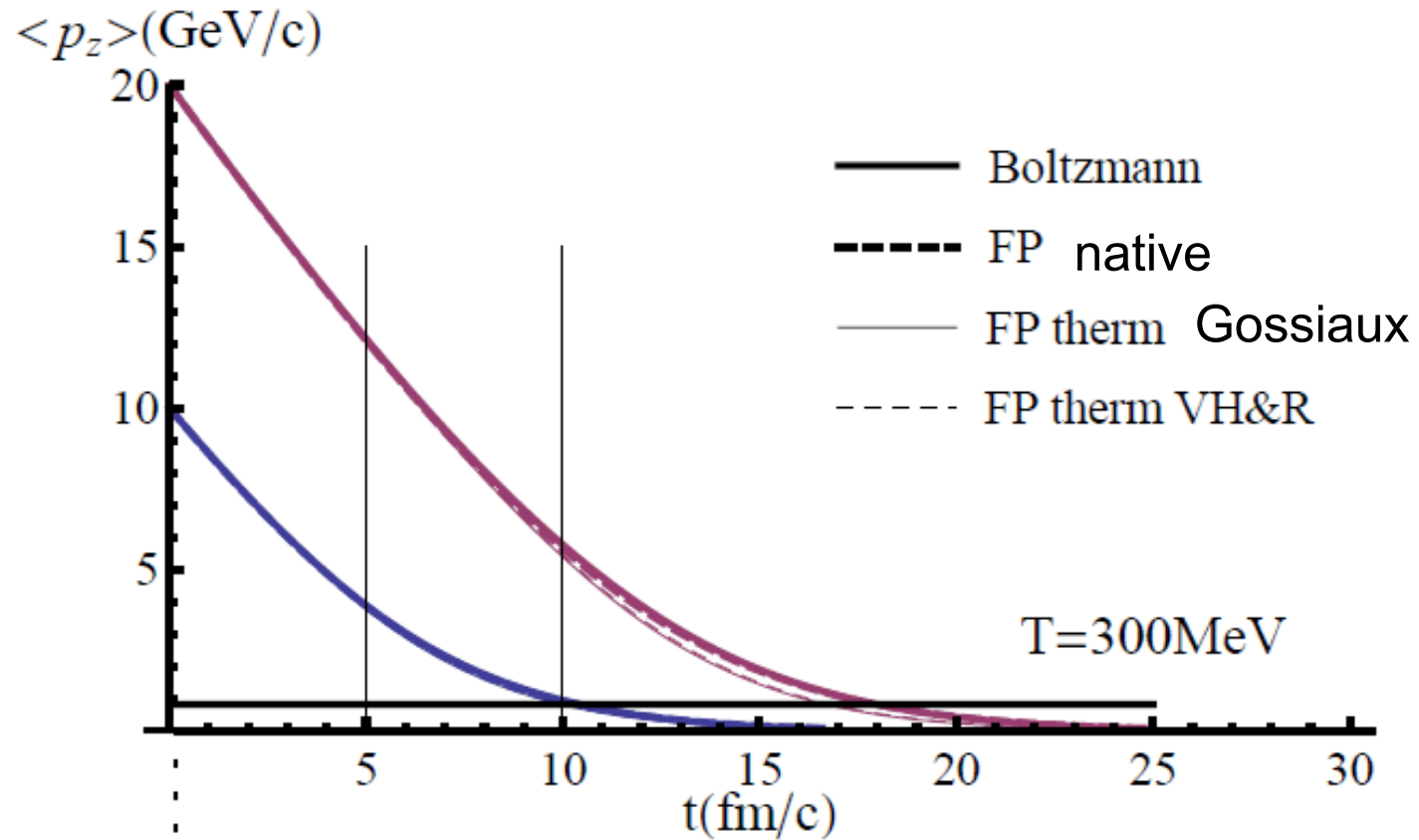
2 corrections prescriptions:

- VHR:  $B_L^{\text{therm VHR}}(p) = E_p T A / p$

- Gossiaux (historical)  $\frac{B_L^{\text{therm}}(p)}{B_T^{\text{therm}}(p)} = \left( \frac{B_L(p)}{B_T(p)} \right)^\beta \quad \beta = 0.25.$



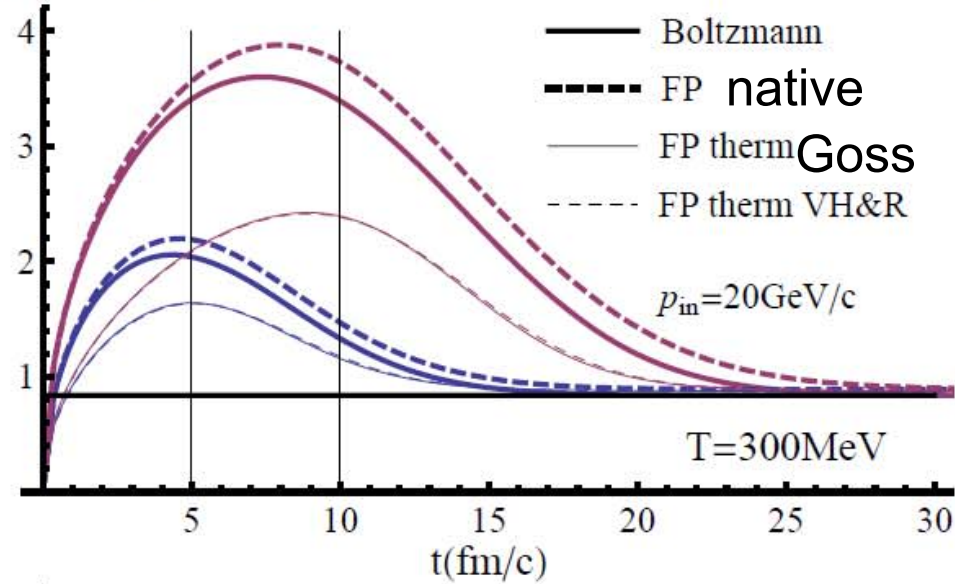
# Boltzmann vs Langevin



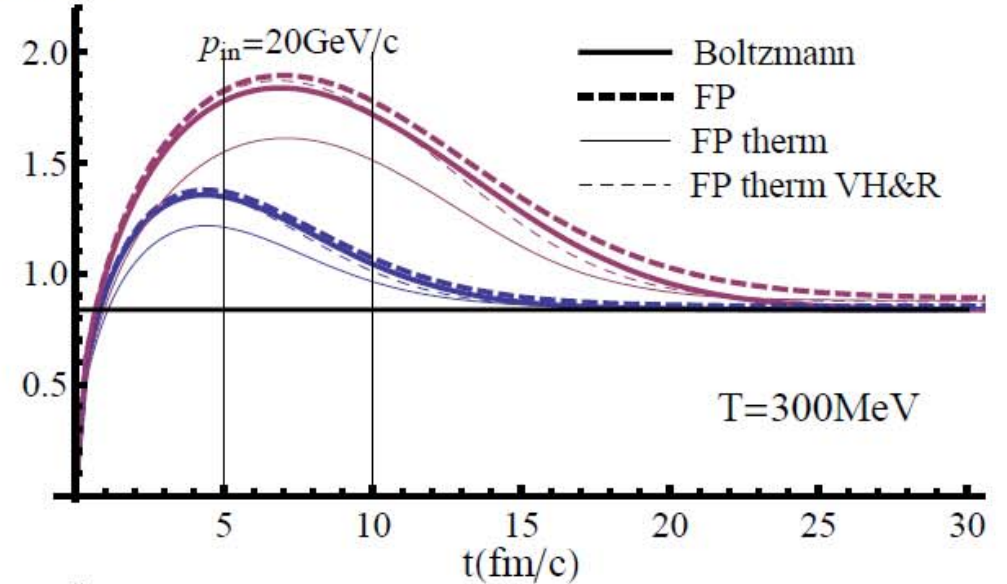


# Boltzmann vs Langevin

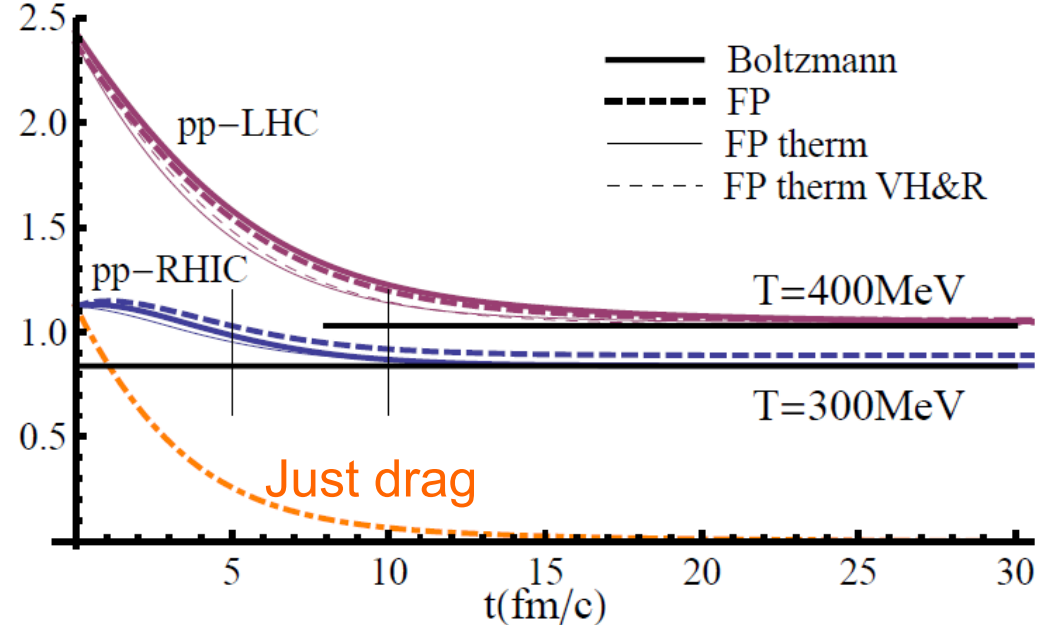
$\sigma(p_z)(\text{GeV}/c)$



$\sigma(p_\perp)(\text{GeV}/c)$

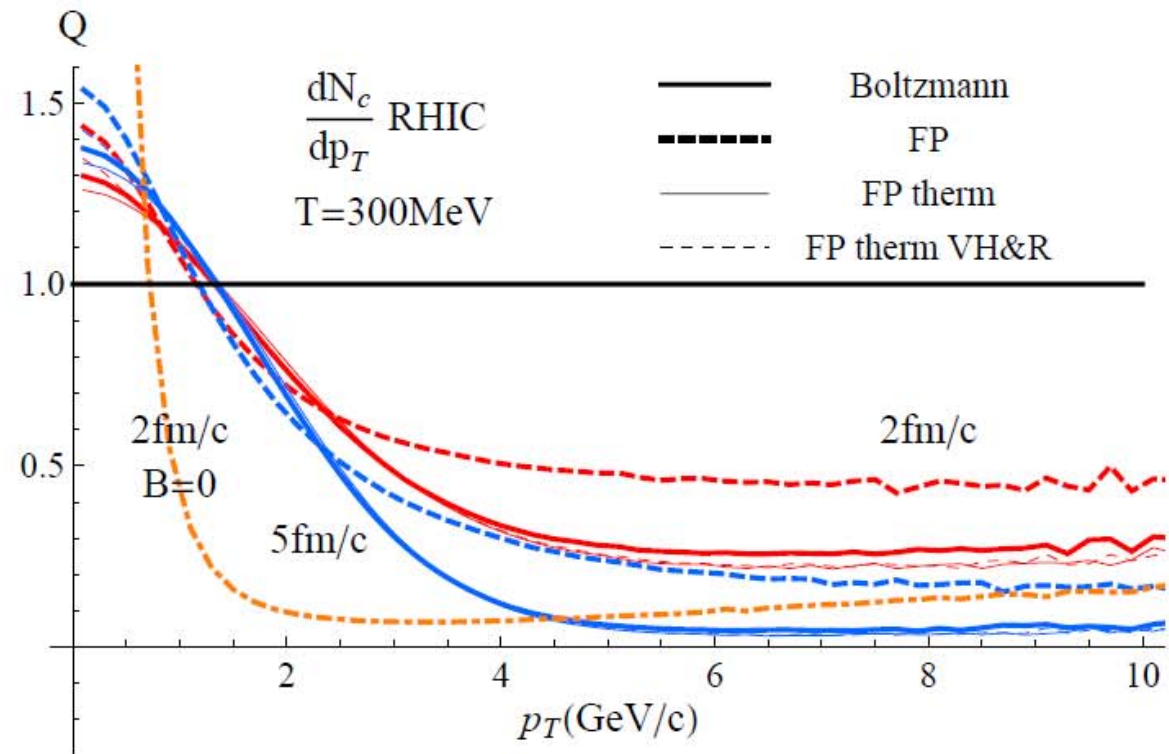
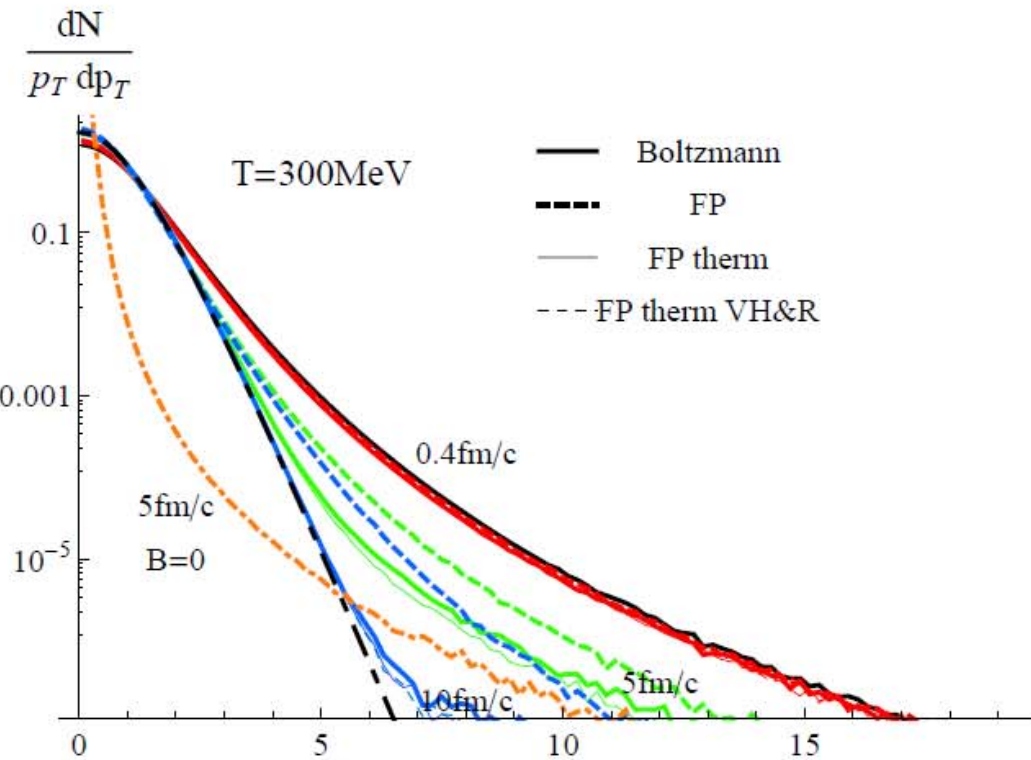


$\sigma(p_T)(\text{GeV}/c)$



# Boltzmann vs Langevin

Evolution in a finite T stationary medium (infinite)

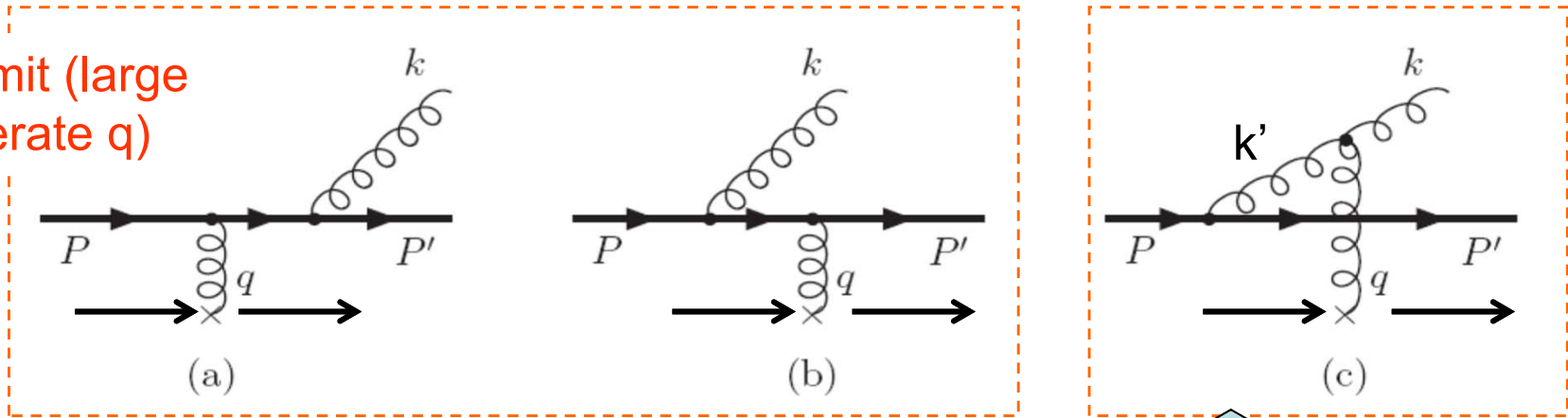


Both tuned FP ok,... Native FP has less RAA (more longitudinal fluctuations dating from Einstein violation)

# Induced Energy Loss

Generalized Gunion-Bertsch (NO COHERENCE) for finite HQ mass, dynamical light partons

Eikonal limit (large E, moderate q)



$$\omega \frac{d^3 \sigma_{\text{rad}}^{x \ll 1}}{d\omega d^2 k_{\perp} dq_{\perp}^2} = \frac{N_c \alpha_s}{\pi^2} (1-x) \times \frac{J_{\text{QCD}}^2}{\omega^2} \times \frac{d\sigma_{\text{el}}^{Qq}}{dq_{\perp}^2}$$

Dominates as small x as one “just” has to scatter off the virtual gluon k’

with

$$\frac{J_{\text{QCD}}^2}{\omega^2} = \left( \frac{\vec{k}_{\perp}}{k_{\perp}^2 + x^2 M^2 + (1-x)m_g^2} - \frac{\vec{k}_{\perp} - \vec{q}_{\perp}}{(\vec{k}_{\perp} - \vec{q}_{\perp})^2 + x^2 M^2 + (1-x)m_g^2} \right)^2$$

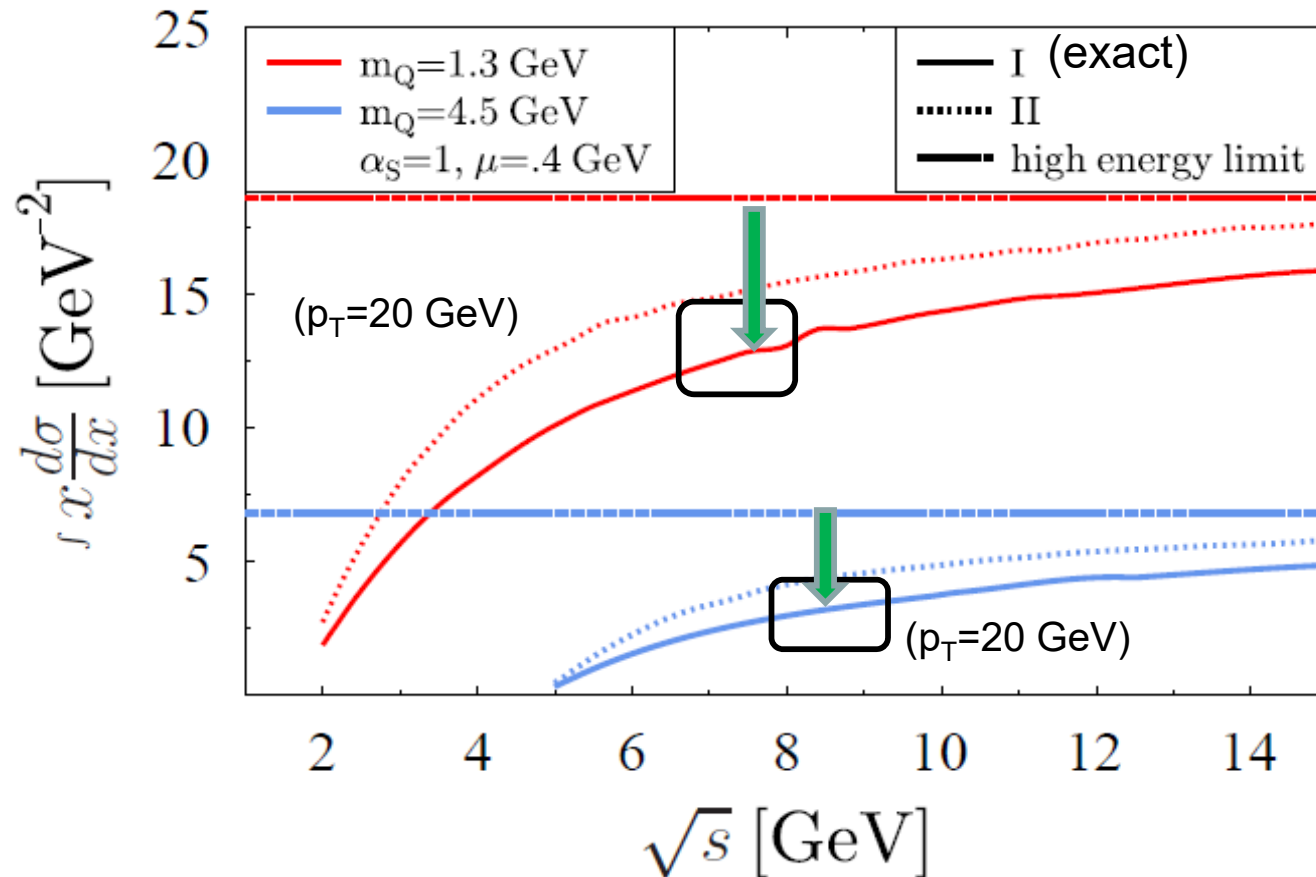
Gluon thermal mass  $\sim 2T$  (phenomenological; not in BDMPS)

Quark mass

Both cures the collinear divergences and influence the radiation spectra (dead cone effect)

# Incoherent Induced Energy Loss

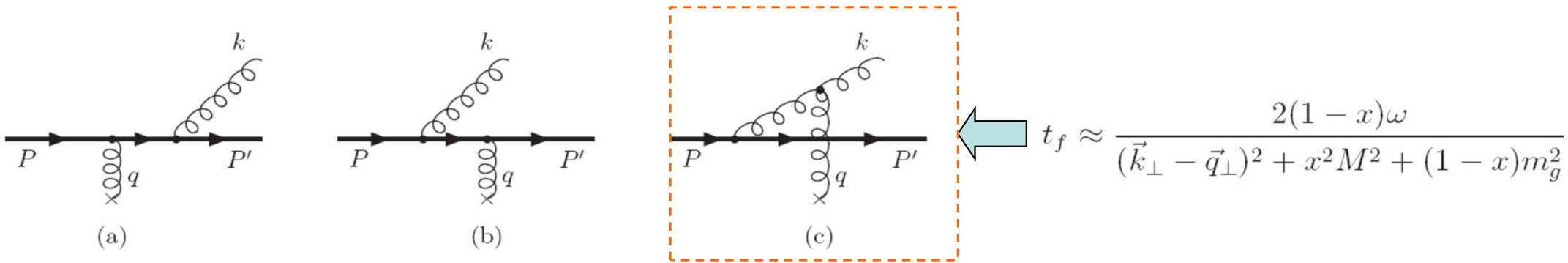
... & finite energy !



Gousset, Gossiaux & Aichelin, Phys. Rev. D 89, 074018 (2014)

Finite energy lead to strong reduction of the radiative energy loss at intermediate  $p_T$

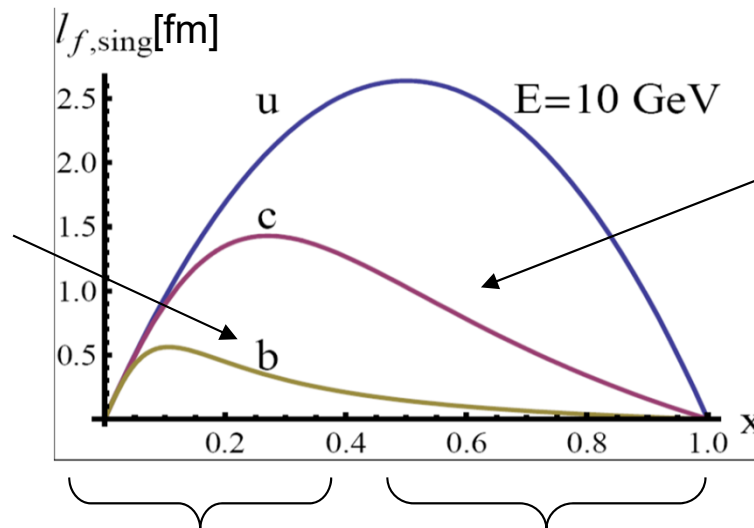
# Formation time for a single coll.



At 0 deflection:

$$l_{f,\text{sing}} \approx \frac{2x(1-x)E}{m_g^2 + x^2 M^2}$$

For  $x < x_{\text{cr}} = m_g/M$ , basically no mass effect in gluon radiation

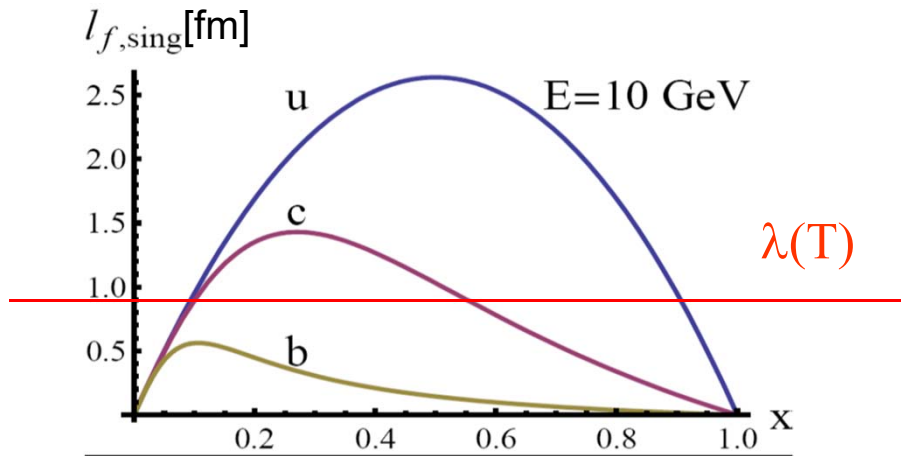


For  $x > x_{\text{cr}} = m_g/M$ , gluons radiated from heavy quarks are resolved in less time than those ← light quarks and gluon ⇒ radiation process less affected by coherence effects in multiple scattering

Dominant region for quenching

Dominant region for average E loss

# A first criteria



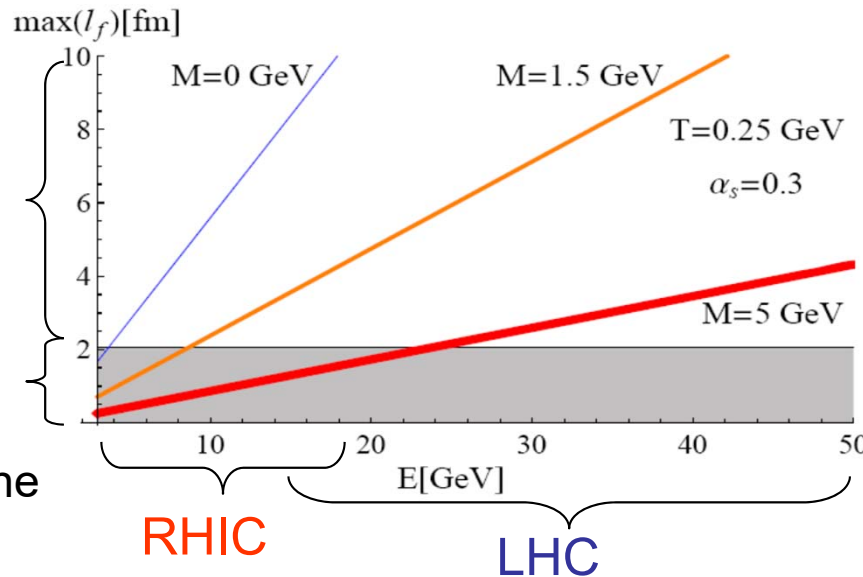
Comparing the formation time (on a single scatterer) with the mean free path:

Coherence effect for HQ gluon radiation :

$$\Leftrightarrow \frac{E}{M} \gtrsim m_g \lambda_Q \sim \frac{1}{g_s}$$

Mostly coherent

Mostly uncoherent



(of course depends on the physics behind  $\lambda_Q$ )

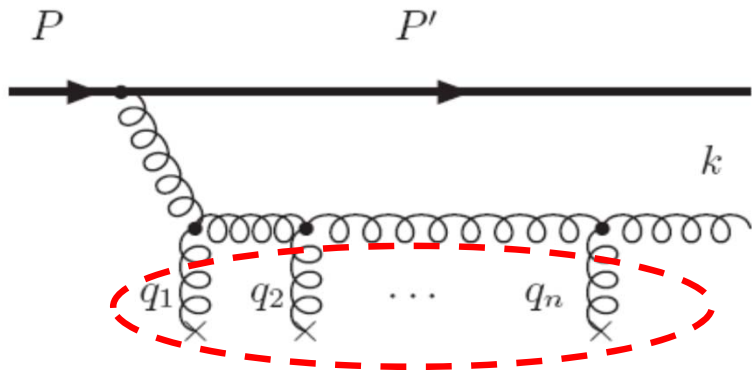
Maybe not completely foolish to neglect coherence effect in a first round for HQ.

(will provide at least a maximal value for the quenching)

# Our basic ingredients for HQ energy loss

## Coherent Induced Radiative

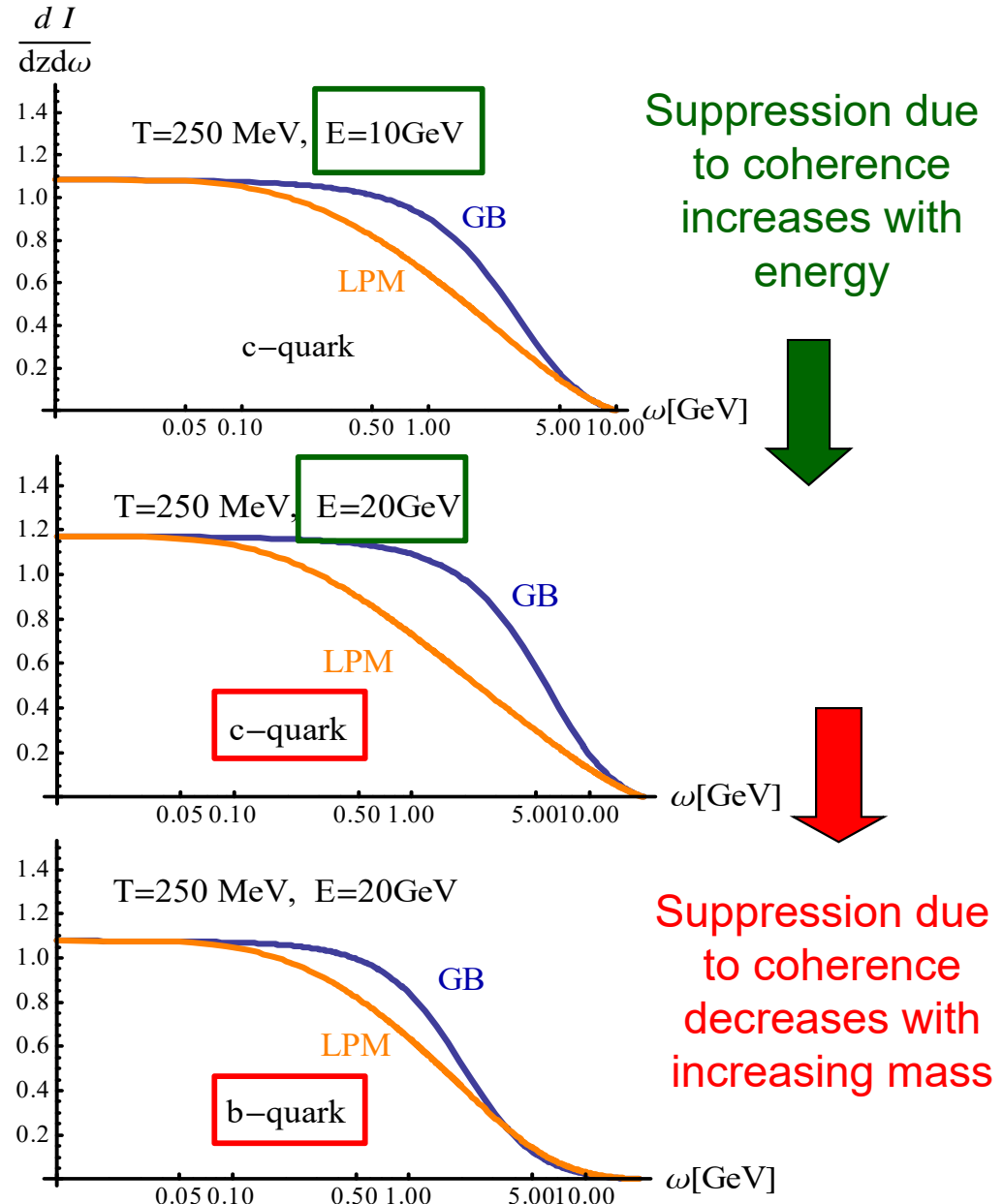
Formation time picture: for  $l_{f,mult} > \lambda$ , gluon is radiated coherently on a distance  $l_{f,mult}$



Model: all  $N_{coh}$  scatterers act as a single effective one with probability  $p_{N_{coh}}(Q_{\perp})$  obtained by convoluting individual probability of kicks

$$\frac{d^2 I_{eff}}{dz d\omega} \sim \frac{\alpha_s}{N_{coh} \tilde{\lambda}} \ln \left( 1 + \frac{N_{coh} \mu^2}{3 (m_g^2 + x^2 M^2 + \sqrt{\omega \hat{q}})} \right)$$

[arXiv:1209.0844] (Hard Probes 2012)





# Monte Carlo Implementation (rad)

I) For each collision with a given  $q_{\perp}$ , we define the conditional probability of radiation:

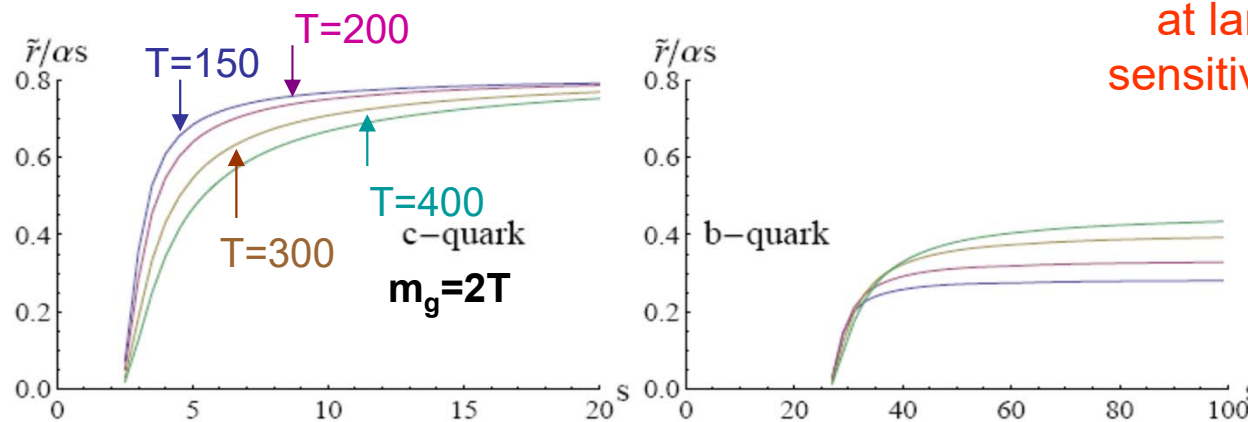
$$r(q_{\perp}) := \frac{\int_0^{+\infty} \frac{d^2\sigma_{\text{rad}}}{d\omega dq_{\perp}^2} d\omega}{\frac{d\sigma_{\text{el}}^{Qq}}{dq_{\perp}^2}}$$

In practice,  $\omega_{\text{min}} = 5\% E$  to avoid IR catastrophe

II) For each collision with a given invariant mass squared  $s$ , we define the conditional *total* probability of radiation:

$$\tilde{r}(s) = \frac{\sigma_{\text{rad}}}{\sigma_{\text{el}}} \approx \frac{\int_{-|t|_{\text{max}}}^0 r(\sqrt{-t}) \frac{d\sigma_{\text{el}}^{Qq}(t)}{dt} dt}{\int_{-|t|_{\text{max}}}^0 \frac{d\sigma_{\text{el}}^{Qq}(t)}{dt} dt}$$

Probes the elastic cross section at larger values of  $t \Rightarrow$  less sensitive to  $\alpha_{\text{eff}}$  at small  $t$ -values



Threshold for radiation



# Monte Carlo Implementation (rad)

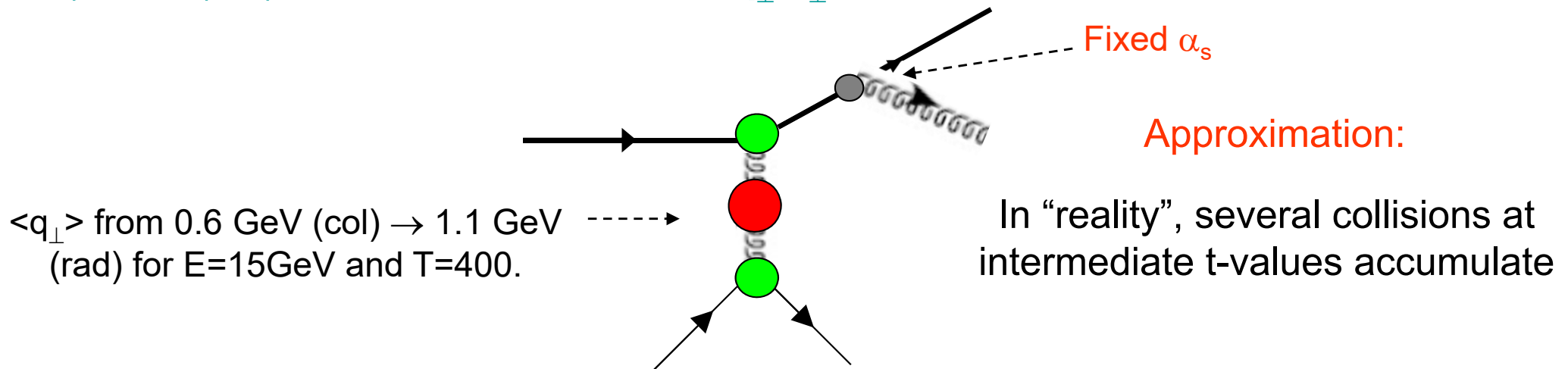
III) For a given HQ energy  $E$ , we sample the entrance channel according to the thermal distribution of light quarks and gluons and  $\sigma_{el}(s)$  and accept according to the conditional probability  $\tilde{r}(s)$

IV) We sample “downwards”  $q_{\perp}$ ,  $\omega$  and then  $k_{\perp}$



Hard shocks with  $|t| > 25\%$   $s$  are rejected (not treated properly in our formalism)

V)  $P^+ \rightarrow (1-x) P^+$  and transverse kick of  $q_{\perp} - k_{\perp}$ .



VI) Reject if out of phase-space